

# Photospheric Magnetic Evolution in the WHI Active Regions

B.T. Welsch · S. Christe · J.M. McTiernan

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**Abstract** Sequences of line-of-sight (LOS) magnetograms recorded by the *Michelson Doppler Imager* are used to quantitatively characterize photospheric magnetic structure and evolution in three active regions that rotated across the Sun’s disk during the Whole Heliosphere Interval (WHI), in an attempt to relate the photospheric magnetic properties of these active regions to flares and coronal mass ejections (CMEs). Several approaches are used in our analysis, on scales ranging from whole active regions, to magnetic features, to supergranular scales, and, finally, to individual pixels. We calculated several parameterizations of magnetic structure and evolution that have previously been associated with flare and CME activity, including total unsigned magnetic flux, magnetic flux near polarity-inversion lines, amount of canceled flux, the “proxy Poynting flux,” and helicity flux. To catalog flare events, we used flare lists derived from both GOES and RHESSI observations. By most such measures, AR 10988 should have been the most flare- and CME-productive active region, and AR 10989 the least. Observations, however, were not consistent with this expectation: ARs 10988 and 10989 produced similar numbers of flares, and AR 10989 also produced a few CMEs. These results highlight present limitations of statistics-based flare and CME forecasting tools that rely upon line-of-sight photospheric magnetic data alone.

**Keywords** Flares, dynamics · Helicity, magnetic · Magnetic fields, corona

## 1. Characterizing Photospheric Magnetic Evolution

Evolution of magnetic fields in solar active regions (ARs) affects the heliosphere in many ways. In the low corona, sudden magnetic evolution in flares and coronal mass ejections

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B.T. Welsch (✉) · J.M. McTiernan  
Space Sciences Laboratory, University of California, 7 Gauss Way, Berkeley, CA 94720-7450, USA  
e-mail: [welsch@ssl.berkeley.edu](mailto:welsch@ssl.berkeley.edu)

S. Christe  
NASA/Goddard Space Flight Center, Greenbelt, MD 20771, USA

(CMEs) – which arise on timescales of minutes to hours – can launch powerful disturbances into interplanetary space. More gradual magnetic evolution, such as the effective diffusion and transport of active-region magnetic flux over the photosphere, also drives evolution in heliospheric structure (affecting, *e.g.*, the structure of the streamer belt and the heliospheric current sheet), on typical timescales of weeks and months. Consequently, studying the evolution of active-region magnetic fields is crucial to understanding the structure and dynamics of the heliosphere, beyond understanding solar activity itself.

Quantifying evolution of magnetic fields in photospheric magnetograms, in particular, can provide insights into heliospheric evolution. Photospheric magnetograms reveal cross sections of the large-scale structure of active regions, which extend from the solar interior out into the corona. The coupling of the photospheric field to the coronal field implies that magnetic evolution at the photosphere will induce evolution in the coronal field. Note, however, that the coronal magnetic field can evolve independently of the photospheric field; for instance, MHD instabilities that arise in the coronal field might trigger flares or CMEs (see, *e.g.*, Forbes, 2000).

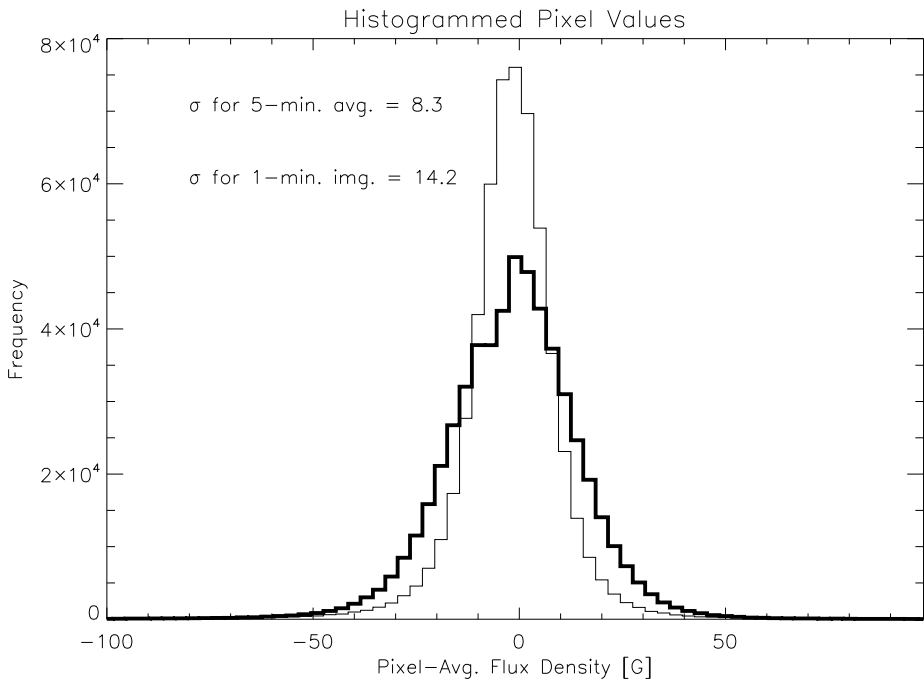
Here, we present analyses of several aspects of photospheric magnetic evolution in the three active regions (NOAA ARs 10987, 10988, and 10989) that crossed the solar disk during the Whole Heliosphere Interval (WHI), as observed in line-of-sight (LOS) magnetograms recorded with the *Michelson Doppler Imager* (MDI) instrument (Scherrer *et al.*, 1995) on the SOHO spacecraft. The data are described in Section 2, our analysis methods and results are discussed in Section 3, and we conclude by discussing the implications of these results in Section 4.

## 2. Data

### 2.1. Magnetograms

Our analysis of photospheric magnetic evolution in the WHI ARs began with selection of magnetograms from the database of full-disk, line-of-sight, 96-minute-cadence, Level 1.8.2 magnetograms from MDI (<http://soi.stanford.edu/magnetic/Lev1.8/>). These magnetograms are formed either from a single measurement, nominally of 30 seconds, or by summing measurements over five minutes. The 30-second magnetograms are much more common in the dataset than the five-minute magnetograms; and the former are noisier. To estimate the noise levels in each, we fit Gaussians to histograms of field strengths (which are actually pixel-averaged flux densities) in one sample magnetogram of each type, and took the noise level as  $1\sigma_{\text{fit}}$ . Each sample magnetogram was smoothed with a 2D, three-pixel boxcar prior to histogramming into 3 G bins. While we expect noise to dominate the weakest-field pixels, and would therefore prefer to fit only the “core” of each histogram (Hagenaar *et al.*, 1999), in practice using ranges smaller than  $\pm 30$  G resulted in poor fits. Results fitting this range of field strengths differed little from those derived by fitting the whole histogram. Whole-histogram  $\sigma_{\text{fit}}$  values were  $\approx 14$  G and  $\approx 8$  G for single and five-measurement magnetograms, respectively; the sample histograms used are plotted in Figure 1. Given the scarcity of the five-minute magnetograms, we assume a single noise level of 14 G for simplicity.

The MDI instrument measures the LOS field strength [ $B_{\text{LOS}}$ ] averaged over each pixel. Tracking the evolution of the radial magnetic field [ $B_R$ ] requires estimating  $B_R$ , since only  $B_{\text{LOS}}$  was observed. We therefore assumed that the magnetic field was radial, and applied cosine corrections to the LOS field in each pixel,  $B_R = B_{\text{LOS}} / \cos(\gamma)$ , where  $\gamma$  is the heliocentric angle from disk center to each pixel. To compensate for foreshortening, triangulation



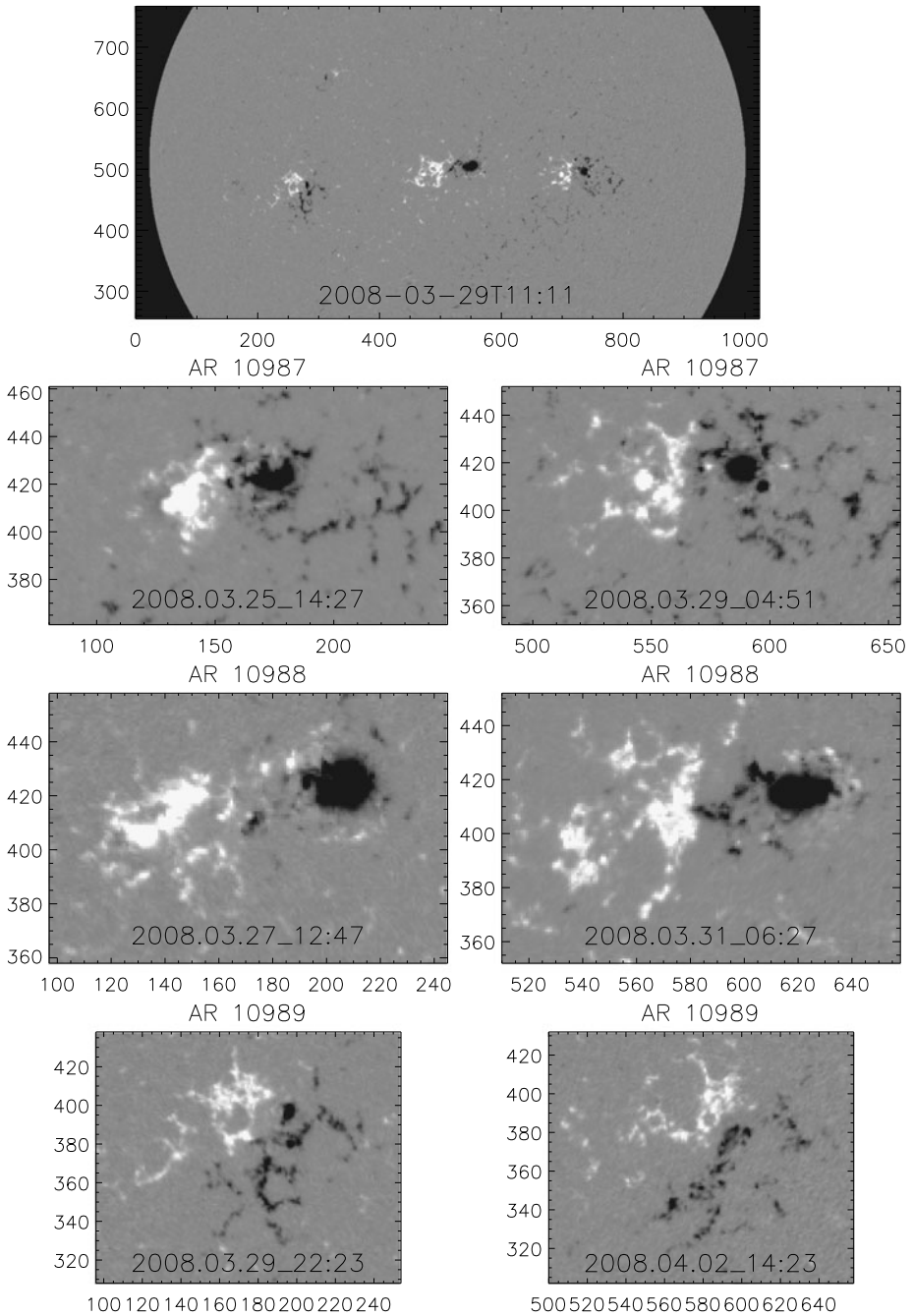
**Figure 1** Histograms of pixel-average field strengths in single- (thick) and five-measurement (thin) magnetograms. Gaussian fits to the histograms can be used to estimate the noise levels in each, which are  $\approx 14$  G and  $\approx 8$  G, respectively.

**Table 1** Intervals over which photospheric magnetic fields of WHI ARs were tracked on the central disk.

NOAA AR	Tracking Start	Tracking End
10987	24 March 2008, 14:23 UT	30 March 2008, 04:47 UT
10988	26 March 2008, 12:48 UT	01 April 2008, 06:23 UT
10989	28 March 2008, 22:23 UT	03 April 2008, 14:23 UT

was used to interpolate the  $B_R$  data – regularly gridded in the plane of the sky, but irregularly gridded in spherical coordinates ( $\theta, \phi$ ) on the solar surface – onto points ( $x, y$ ) corresponding to a regularly gridded Mercator projection of the spherical surface, following Welsch *et al.* (2009). This projection is conformal (and so locally preserves shape), which is necessary to ensure displacements measured by our tracking methods were not biased in direction. This reprojection distorts length scales, such that apparent displacements are exaggerated by a factor of the secant of the apparent latitude, which we corrected after tracking.

Since the MDI magnetograph only measures the LOS component of the photospheric magnetic field, we chose to analyze only magnetograms in which the target AR was within about  $45^\circ$  of disk center. The first AR visible on the disk during WHI was AR 10987 on 24 March 2008, and we started our tracking analyses with the magnetogram recorded at 14:23 UT. Shortly thereafter, AR 10988 rotated onto the disk, followed by AR 10989. By 2 April, AR 10989 had no sunspots, but we analyzed magnetograms through 4 April, when AR 10989 was nearly  $45^\circ$  from disk center, ending at 14:23 UT. The time ranges over which each AR was tracked are listed in Table 1. The top-most magnetogram in Figure 2 shows all



**Figure 2** Top: This full-disk magnetogram, cropped at  $\pm 30^\circ$ , shows all three WHI ARs (from right to left, 10987, 10988, 10989). The cropped magnetograms in each of the subsequent rows show each AR roughly one day after we began tracking it (left) and one day before we stopped tracking it (right). Axes' labels are arc pixels from MDI full-disk magnetograms.

three WHI ARs on the disk. The magnetograms in each of the subsequent rows of the same Figure show each WHI AR roughly one day after we began tracking it (left) and one day before we stopped tracking it (right).

## 2.2. Flare and CME Activity

Our primary goal is to relate properties of magnetic structure and evolution at the photosphere to energy release in the corona, in the form of flares and CMEs.

Webb *et al.* (2011) used several sources of data to compile a comprehensive list of CMEs over the WHI, and to determine their source regions. We used their results to determine CME productivity of the WHI ARs while we tracked them. Only AR 10989 was CME productive while tracked; it produced two during its tracking interval (and a further two in the hours just outside the interval over which it was tracked).

While CMEs are generally responsible for the strongest heliospheric disturbances (Gosling, 1993), flares can also affect the heliosphere. As detailed below, each WHI AR only produced relatively small flares during the interval over which it was tracked. But even weak flares can affect the heliosphere: for instance, small hard X-ray (HXR) bursts are often associated with interplanetary Type III radio bursts (see, *e.g.*, Christe, Krucker, and Lin, 2008), which arise from electrons escaping into the heliosphere (where they have been observed *in situ*).

To characterize flare activity in the WHI ARs, we first consulted records of soft X-ray (SXR) flare emission observed with the GOES satellites in the flare catalog maintained by NOAA ([ftp://ftp.ngdc.noaa.gov/STP/SOLAR\\_DATA/SOLAR\\_FLARES/FLARES\\_XRAY/](ftp://ftp.ngdc.noaa.gov/STP/SOLAR_DATA/SOLAR_FLARES/FLARES_XRAY/)), and we found that most of the relatively weak flares during WHI were not attributed to any source region, meaning this catalog did not accurately characterize each AR's flare activity. Next, we consulted Sam Freeland's Latest Events Archive (LEA: [http://www.lmsal.com/solarsoft/latest\\_events\\_archive.html](http://www.lmsal.com/solarsoft/latest_events_archive.html)) which differences EUV images to determine flare-source locations. The LEA flare list identified the source ARs for many events that lacked source ARs in the GOES catalog. In the three cases where the NOAA and LEA source attributions disagreed, manual inspection of LEA difference images suggested the LEA attributions were probably correct. Some flares in the LEA list were incorrectly attributed to either: *i*) remnant ARs from previous rotations that were due to rotate back to the flares' positions when they occurred, or *ii*) ARs farther West than the true source AR. Both errors might arise from using active region locations from Solar Region Summaries (SRSs), jointly prepared once per day by NOAA's Space Weather Prediction Center (SWPC; <http://www.swpc.noaa.gov/ftpdir/forecasts/SRS/README>) and the US Air Force, that were issued many hours before the flare time. While source latitudes and longitudes in the LEA list appear accurate for the events that we studied, AR source attributions from both the NOAA and LEA event lists contain errors.

A more robust approach to automatic identification of flares' source active regions uses data from the RHESSI satellite (Lin *et al.*, 2002), which is capable of localizing the source regions of hard X-rays (HXRs) emitted in flares (as well as imaging HXR emission in high-fluence flares). Recent improvements in the algorithms used to identify microflares (short bursts of HXR emission in RHESSI's 6–12 keV energy band; see, *e.g.*, Christe *et al.*, 2008), which are invariably associated with active regions, has enabled their inclusion in the most recent RHESSI flare catalog ([http://hessi.ssl.berkeley.edu/hessidata/dbase/hessi\\_flare\\_list.txt](http://hessi.ssl.berkeley.edu/hessidata/dbase/hessi_flare_list.txt)). To find the source AR for each flare in the RHESSI catalog, disk positions for the WHI ARs from the daily SRSs were used to develop linear models of for each AR's apparent latitude and longitude as a function of time. This approach enabled

extrapolating the positions of ARs both before they were visible near the east limb and recognized as new ARs, and after they passed beyond the west limb. Flares were automatically associated by proximity to the nearest predicted AR location. Visual inspection of each automatic association confirmed that this method correctly assigned above-the-limb flares to ARs which, though not visible, were at or near the limb. Lightcurves from GOES were then searched to identify the transient X-ray enhancement associated with each RHESSI flare, and the enhancement's peak intensity was recorded.

Flares and source AR attributions are listed in Table 2, and plotted in Figure 3, which shows the position of each RHESSI flare with respect to the solar disk, and its AR association. We note that most of the flares for AR 10988 occurred on the eastern disk, and many of the flares for 10989 occurred above the east limb. Consequently, the LOS magnetograms from MDI cannot tell us much about the photospheric magnetic structure of these ARs during their most flare-productive intervals.

In Table 3, we summarize flare and CME activity for each WHI AR separately for two time intervals: first, over the whole time range from appearance over the east limb to its disappearance around the west limb; and second, during the limited time interval that the AR was tracked. Times and source ARs for CMEs were taken from Webb *et al.* (2011). Not counting RHESSI flares for which a peak in the GOES lightcurve could not be automatically isolated, we found that ARs 10987, 10988, and 10999 produced 30, 44, and 28 flares, respectively, as they crossed the disk, and 9, 11, and 5 flares, respectively, while they were tracked across the central disk. Abramenko (2005) used a weighted, time-average of each AR's flare X-ray fluxes observed by GOES as a "flare index" to quantify AR flare activity; consistent with the definition of GOES flare classes, a power of ten difference in weighting was used between flare classes. Given such a weighting, the M- and C-class flares produced by AR 10989 imply that its average flare flux greatly exceeds that of the other two ARs during either of the intervals in Table 3.

### 3. Analysis of Magnetic Structure and Evolution

We quantitatively analyzed magnetic evolution in these three ARs in several ways, which we present roughly in order of decreasing length scale: starting from whole-active-region measures of magnetic structure and evolution, we consider evolution on progressively smaller spatial scales, down to individual MDI pixels.

#### 3.1. Large-Scale Structure and Evolution

Barnes and Leka (2008), Leka and Barnes (2007), and Welsch *et al.* (2009) have noted that total unsigned radial magnetic flux [ $\Phi$ ] in an AR is strongly correlated with its flare productivity.

We calculated the total unsigned estimated radial flux [ $\Phi = \int dA |B_R|$ ] in each of the WHI ARs over the time interval that each was tracked, compensating for distortion in pixel areas due to the Mercator projection. These unsigned fluxes are plotted in Figure 4. The average values of unsigned flux for ARs 10987, 10988, and 10989 were 1.6, 2.0, and  $1.2 \times 10^{22}$  Mx, respectively, over the interval when each was tracked. To minimize the effects of noise, only pixels with unsigned field strength greater than 40 G were included in the sums; this is approximately three times our assumed noise level of 14 G. Assuming the uncorrelated, uniform per-pixel noise level on flux of  $\sigma_0 = 14 \text{ G } (\Delta x)^2$ , where  $\Delta x$  is the width of MDI full-disk pixels, a formal estimate of the error in total flux would be  $\sigma_{\text{sum}} = \sqrt{N_{>40\text{G}}}\sigma_0$ ;

**Table 2** RHESSI/HXR bursts in the 6–12 keV channel during the WHI interval from the RHESSI flare list. Only those events with valid positions are shown in this list. Positions are listed in heliographic coordinates (in degrees) if on the disk or in heliocentric coordinates (in arcseconds) if above the limb. The associated GOES class is also shown for each event; some events occurred during GOES data gaps.

#	Date	Start	Stop	Peak	Coordinates	GOES Class	Source AR
1	23 March 2008	18:51	18:51	18:51	S08E79	A7.9	10988
2	23 March 2008	23:38	23:41	23:39	S08E50	A6.5	10987
3	23 March 2008	23:44	23:48	23:45	S08E51	B1.4	10987
4	23 March 2008	23:51	23:51	23:51	S07E50	A6.4	10987
5	24 March 2008	00:24	00:25	00:25	S08E50	B1.0	10987
6	24 March 2008	01:14	01:16	01:15	S07E48	B1.0	10987
7	24 March 2008	01:18	01:22	01:19	S07E49	B1.8	10987
8	24 March 2008	01:26	01:29	01:27	S08E50	B1.3	10987
9	24 March 2008	01:32	01:33	01:32	S08E50	B1.1	10987
10	24 March 2008	01:47	01:50	01:48	S08E76	A9.3	10988
11	24 March 2008	02:46	02:53	02:47	S08E49	B4.6	10987
12	24 March 2008	02:53	02:59	02:54	S08E48	B2.8	10987
13	24 March 2008	02:59	03:11	03:03	S07E47	B4.4	10987
14	24 March 2008	06:45	06:49	06:48	S07E44	A8.9	10987
15	24 March 2008	07:59	08:10	08:04	S07E45	B2.3	10987
16	24 March 2008	08:10	08:36	08:16	S07E46	B3.3	10987
17	24 March 2008	10:08	10:10	10:09	S07E43	A7.0	10987
18	24 March 2008	11:36	11:39	11:37	S08E71	A7.7	10988
19	24 March 2008	11:39	11:44	11:39	S08E68	A6.4	10988
20	24 March 2008	12:56	12:57	12:56	S07E42	A7.1	10987
21	24 March 2008	13:05	13:06	13:06	S08E67	A8.5	10988
22	24 March 2008	14:04	14:07	14:06	S08E67	B1.1	10988
23	24 March 2008	14:47	14:49	14:48	S09E69	A7.2	10988
24	24 March 2008	14:53	14:58	14:55	S09E68	A7.9	10988
25	24 March 2008	15:40	15:41	15:40	S08E66	A7.2	10988
26	24 March 2008	15:56	15:58	15:57	S08E67	B1.0	10988
27	24 March 2008	16:14	16:21	16:16	S07E40	B1.2	10987
28	24 March 2008	17:13	17:14	17:13	S08E65	A9.5	10988
29	24 March 2008	17:34	17:38	17:34	S08E65	A9.4	10988
30	24 March 2008	19:08	19:13	19:09	−964,−197	B1.0	10989
31	24 March 2008	20:52	20:54	20:53	S07E37	B1.3	10987
32	24 March 2008	21:58	22:04	21:59	S07E63	B1.7	10988
33	25 March 2008	01:59	02:02	02:00	S07E59	B1.4	10988
34	25 March 2008	04:27	04:30	04:28	S07E59	no data	10988
35	25 March 2008	04:30	04:31	04:31	S07E59	no data	10988
36	25 March 2008	04:50	05:07	04:54	−966,−182	B5.2	10989
37	25 March 2008	07:53	08:04	08:01	−943,−207	B1.8	10989
38	25 March 2008	09:31	09:35	09:34	−949,−172	B1.1	10989
39	25 March 2008	11:18	11:28	11:20	−958,−139	B1.7	10989
40	25 March 2008	13:18	13:22	13:21	S08E53	B1.2	10988

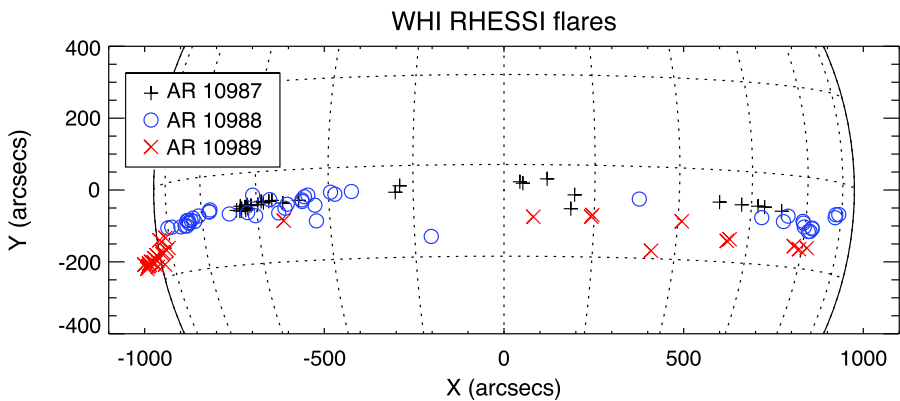
**Table 2** (Continued.)

#	Date	Start	Stop	Peak	Coordinates	GOES Class	Source AR
41	25 March 2008	14:44	14:47	14:45	S06E47	B1.4	10988
42	25 March 2008	14:49	14:54	14:52	S11E84	B2.3	10989
43	25 March 2008	16:10	16:12	16:10	S09E82	B1.1	10989
44	25 March 2008	16:12	16:19	16:15	S08E48	B1.1	10988
45	25 March 2008	17:36	17:41	17:38	S11E81	B2.4	10989
46	25 March 2008	18:44	19:28	18:51	-950,-178	M1.7	10989
47	25 March 2008	19:28	19:30	19:30	-973,-189	C3.4	10989
48	25 March 2008	20:20	20:28	20:21	-974,-200	B9.1	10989
49	25 March 2008	21:06	21:08	21:08	-982,-199	B4.9	10989
50	25 March 2008	21:56	22:12	21:57	-987,-204	B3.4	10989
51	25 March 2008	22:12	22:27	22:18	-989,-211	B3.1	10989
52	25 March 2008	22:27	22:43	22:29	-990,-213	B2.8	10989
53	25 March 2008	22:43	22:47	22:47	-985,-208	B2.5	10989
54	25 March 2008	23:32	23:42	23:35	-992,-219	B2.7	10989
55	26 March 2008	01:08	01:14	01:08	-100,-207	B1.5	10989
56	26 March 2008	01:21	01:23	01:22	-963,-213	B1.4	10989
57	26 March 2008	03:00	03:06	03:01	S09E47	B1.3	10988
58	26 March 2008	03:28	03:29	03:28	S07E18	B1.3	10987
59	26 March 2008	05:19	05:20	05:20	S06E18	B1.0	10987
60	26 March 2008	06:28	06:29	06:29	S07E43	B1.1	10988
61	26 March 2008	07:59	08:01	07:59	S09E41	A9.0	10988
62	26 March 2008	11:23	11:29	11:25	S08E40	B1.9	10988
63	26 March 2008	14:21	14:34	14:21	S08E39	B1.0	10988
64	26 March 2008	17:07	17:17	17:10	S07E36	B1.2	10988
65	26 March 2008	18:53	19:07	18:55	S07E36	B1.3	10988
66	26 March 2008	19:07	19:13	19:09	S06E35	B1.2	10988
67	26 March 2008	19:17	19:21	19:19	S07E35	B1.3	10988
68	27 March 2008	01:35	01:37	01:35	S11E33	A8.6	10988
69	27 March 2008	02:42	02:51	02:43	S06E30	B1.5	10988
70	27 March 2008	03:36	03:37	03:36	S08E33	no data	10988
71	27 March 2008	05:17	05:19	05:18	S07E29	A8.9	10988
72	27 March 2008	11:10	11:13	11:10	S06E26	A8.1	10988
73	27 March 2008	15:50	15:53	15:50	S05W03	B1.3	10987
74	27 March 2008	16:19	16:20	16:19	S06W03	B1.5	10987
75	28 March 2008	01:11	01:15	01:11	S05W07	A6.5	10987
76	28 March 2008	09:39	09:48	09:44	S10W11	B1.6	10987
77	28 March 2008	10:44	10:46	10:45	S07W12	A7.2	10987
78	28 March 2008	14:01	14:10	14:03	S14E13	B1.2	10988
79	28 March 2008	15:27	15:28	15:28	S10E40	A5.8	10989
80	30 March 2008	07:55	07:56	07:55	S07W39	A5.6	10987
81	30 March 2008	17:32	17:36	17:36	S07W44	B1.3	10987
82	30 March 2008	20:33	20:36	20:33	S07W48	A8.5	10987
83	30 March 2008	23:25	23:29	23:26	S07W49	A8.3	10987



**Table 2** (Continued.)

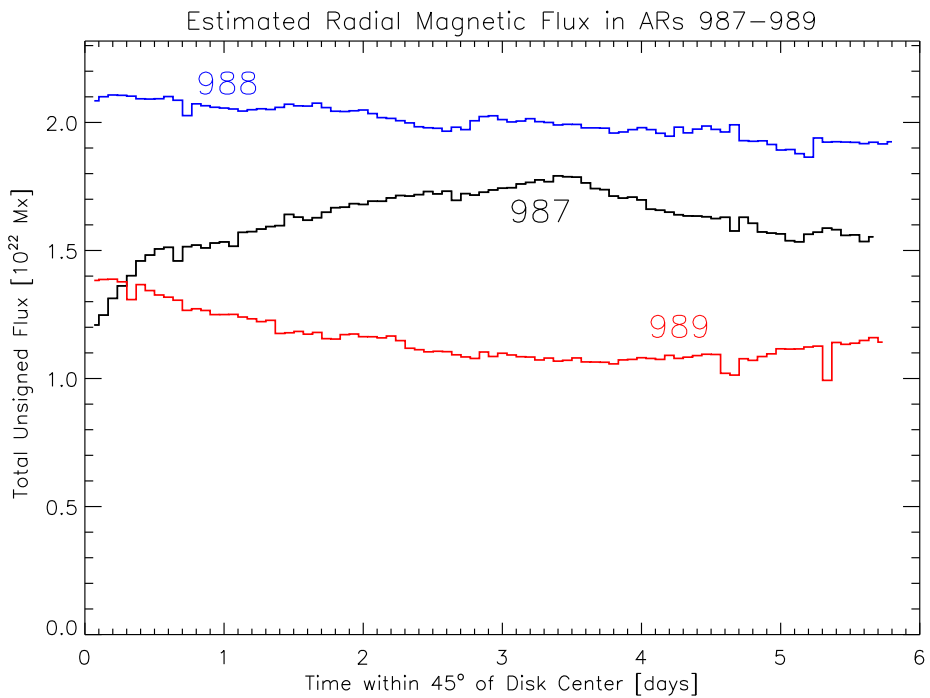
#	Date	Start	Stop	Peak	Coordinates	GOES Class	Source AR
84	31 March 2008	06:05	06:06	06:05	S07W54	A8.3	10987
85	31 March 2008	06:32	06:36	06:33	S08W23	A5.5	10988
86	01 April 2008	00:15	00:16	00:16	S11W05	A7.9	10989
87	01 April 2008	20:15	20:16	20:15	S11W15	A6.5	10989
88	01 April 2008	20:18	20:22	20:20	S10W15	B1.0	10989
89	02 April 2008	03:09	03:15	03:10	S09W49	A4.3	10988
90	02 April 2008	12:34	12:38	12:36	S09W55	A8.6	10988
91	02 April 2008	15:44	15:46	15:45	S08W56	A5.1	10988
92	02 April 2008	16:51	16:58	16:51	S08W61	B1.0	10988
93	02 April 2008	20:03	20:13	20:06	S16W26	B1.1	10989
94	02 April 2008	22:30	22:31	22:30	S09W61	A6.5	10988
95	02 April 2008	23:40	23:53	23:43	S09W62	B2.0	10988
96	03 April 2008	01:12	01:50	01:21	S11W32	C1.2	10989
97	03 April 2008	04:56	04:57	04:57	S10W64	A8.1	10988
98	03 April 2008	05:55	06:02	05:57	S09W65	B1.2	10988
99	03 April 2008	06:02	06:10	06:07	S09W65	A9.9	10988
100	03 April 2008	07:35	07:37	07:36	S10W63	A4.2	10988
101	03 April 2008	20:00	20:11	20:04	S06W77	no data	10988
102	03 April 2008	20:15	20:20	20:17	S13W41	no data	10989
103	03 April 2008	20:20	20:28	20:23	S13W42	no data	10989
104	03 April 2008	22:09	22:14	22:11	S06W75	A8.7	10988
105	03 April 2008	22:22	22:24	22:22	S06W75	A5.8	10988
106	05 April 2008	03:13	03:17	03:13	S13W59	A5.1	10989
107	05 April 2008	05:33	05:37	05:33	S13W61	A6.4	10989
108	05 April 2008	11:02	11:16	11:05	S12W64	B1.3	10989



**Figure 3** Positions and source ARs for flares identified by RHESSI.

**Table 3** Observed flares and CMEs from WHI ARs, from limb to limb (top three rows), and while tracked (bottom three rows). A, B, C, and M denote GOES flare classes. (RHESSEI flares during GOES data gaps are not included in these tallies.) CMEs within a few hours before or after the start or end times shown are included in parentheses before or after the frequency during the interval, respectively. The M- and C-class flares produced by AR 10989 imply that its flare index, a measure of AR flare productivity (Abramenko, 2005), exceeds those of ARs 10987 and 10988.

AR	Start Obs.	End Obs.	A	B	C	M	Tot. Flares	CMEs
10987	23 March, 23:39 UT	05 April, 11:17 UT	11	19			30	0 (1)
10988	23 March, 18:51 UT	05 April, 11:17 UT	24	20			44	(1)4
10989	24 March, 19:09 UT	05 April, 11:17 UT	5	20	2	1	28	8 (1)
10987	24 March, 14:23 UT	30 April, 04:47 UT	2	7			9	0
10988	26 March, 12:48 UT	01 April, 06:23 UT	4	7			11	0
10989	28 March, 22:23 UT	03 April, 14:23 UT	2	2	1		5	(1)2 (1)



**Figure 4** Total unsigned flux [ $\Phi$ ] versus time in the three WHI ARs, as each crossed the central solar disk. Dips arise from lower noise levels in magnetograms averaged over five measurements. Larger values of  $\Phi$  have been associated with greater flare activity.

this is typically  $< 10^{20}$  Mx, which is not visible on these plots. Dips in the plots arise from lower noise levels in magnetograms averaged over five measurements, and give a better estimate of the noise level. Also, the magnetic field is highly correlated from frame to frame at a 96-minute cadence (Welsch *et al.*, 2009), implying that frame-to-frame variations in total flux also indicate noise levels. Note that MDI has a known problem with saturation

in strong-field regions (Liu, Norton, and Scherrer, 2007), such that flux values reported here might be lower than the actual flux (Wang *et al.*, 2009).

Based upon total unsigned flux alone, AR 10988 should have been the most active, and AR 10989 the least.

Schrijver (2007) argued that strong magnetic fields concentrated near polarity-inversion lines (PILs) of the photospheric LOS magnetic field are closely associated with the occurrence of large flares. He developed a method to quantify the total unsigned magnetic flux [ $R$ ] near strong-field polarity-inversion lines (SPILs) of ARs, by generating a weighting map of proximity to SPILs and summing the product of the weighting map and unsigned LOS magnetic flux. Because strong fields along LOS PILs are correlated with strong gradients in LOS fields across PILs (Falconer, Moore, and Gary, 2003), the  $R$ -parameter is quantitatively related to the length of strong-gradient PILs, which has been found by Falconer, Moore, and Gary (2003, 2006) to be associated with CMEs. Barnes and Leka (2008) and Welsch *et al.* (2009) also found  $R$  to be associated with flare activity.

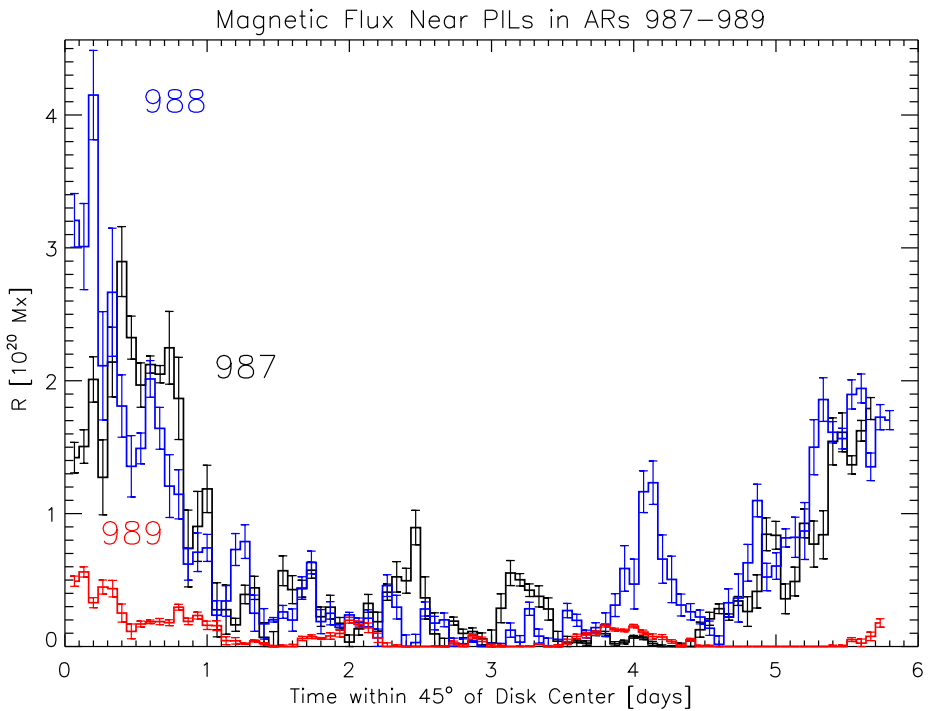
Emulating Schrijver's approach here, we computed  $R$  values for each of the WHI ARs as they crossed the disk, choosing (as he did) a strong-field threshold of 150 G and FWHM of 15 Mm in the Gaussian used in the convolution to compute the SPIL weighting map (see Welsch and Li, 2008 for more details of the procedure). Our results are plotted in Figure 5. Note that our values of  $R$  are in units of Mx; Schrijver's were in units of G, summed over the weighting map. The MDI disk-center pixel area of  $\approx 2.2 \times 10^{16} \text{ cm}^2$  is an approximate conversion factor. Note also that Schrijver (2007) apparently used MDI Level 1.8.0 magnetograms, while we use Level 1.8.2 magnetograms (see <http://soi.stanford.edu/magnetic/Lev1.8/>). Since absolute flux densities in the latter are higher than in the former by a spatially varying factor of approximately 1.6, our  $R$  values cannot easily be compared with Schrijver's. As with estimating total unsigned flux, uncertainties in  $R$  computed assuming an uncorrelated, uniform per-pixel noise level [ $\sigma_0$ ] are too small to be visible on the plot. Instead, we have crudely estimated uncertainties from the  $R$  values themselves by computing the standard error in the mean with a five-point boxcar window. This simplistic approach is reasonable because, as noted by Welsch *et al.* (2009), changes in magnetic fields are relatively minor over a few hours, so successive measurements of  $R$  can be interpreted as repeated, independent measurements of nearly the same physical value.

As with total unsigned flux, expectations of flare activity based upon  $R$  values would suggest AR 10988 should be most active, and AR 10989 should be least active.

### 3.2. Intermediate-Scale Evolution: Feature Tracking

Automated tracking of "features" in magnetogram sequences has been used to understand processes governing evolution of the photospheric magnetic field, including flux emergence and dispersal (*e.g.* DeForest *et al.*, 2007 and references therein). Features in magnetograms have been identified in several ways, for instance by: "clumping" collections of contiguous, like-polarity, above-threshold pixels (see, *e.g.*, Parnell *et al.*, 2009); "downhill" segmentation, which identifies distinct "hilltops" in absolute field strength (see, *e.g.*, Welsch and Longcope, 2003); and curvature, identifying the convex cores of hilltops in absolute field strength (*e.g.* Hagenaar *et al.*, 1999). Tracking involves the association of identified features between successive frames.

Feature tracking can be used to identify episodes of flux cancellation, in which closely spaced, opposite-polarity features simultaneously appear to lose flux (Livi, Wang, and Martin, 1985). Since flux cancellation has been observed in prominence formation (Martin,

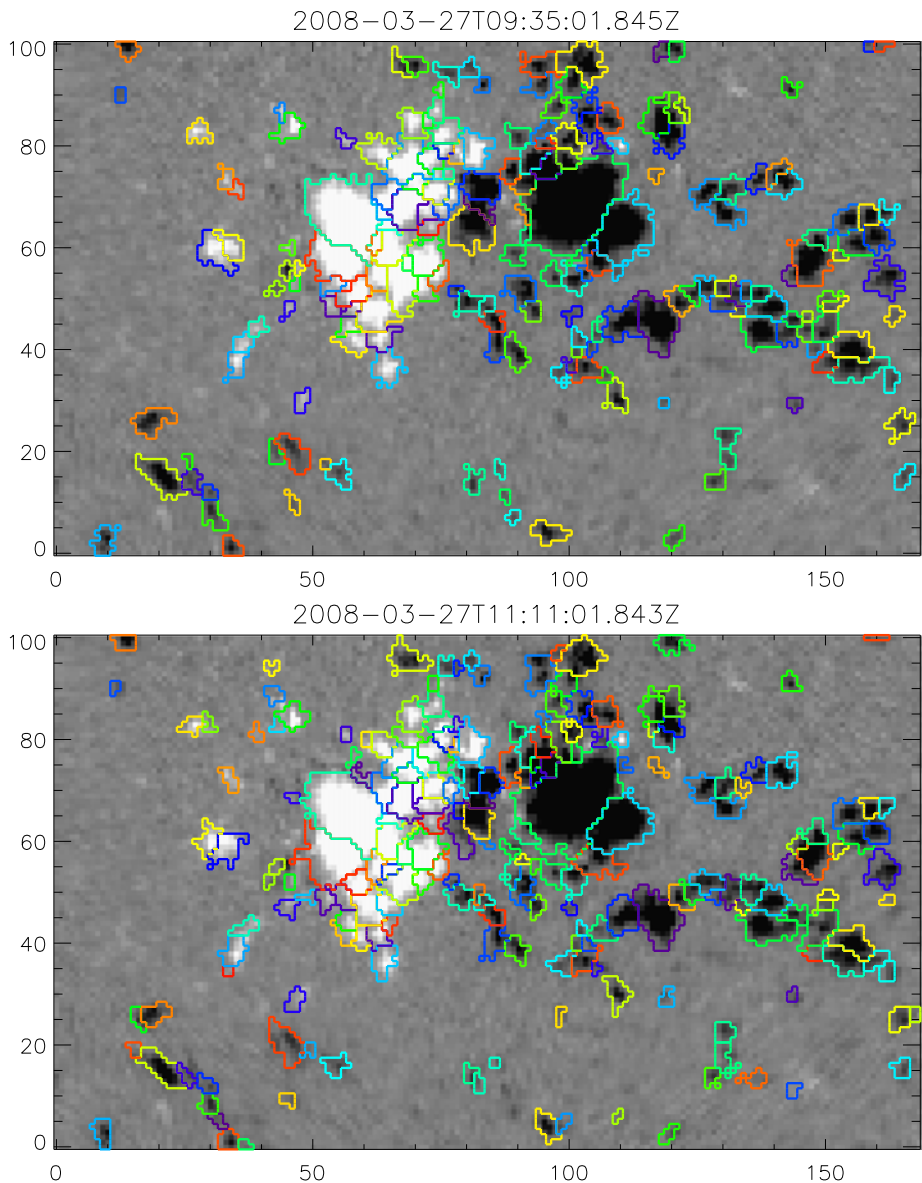


**Figure 5** Total unsigned flux [ $R$ ] near strong-field polarity-inversion lines (SPILs) versus time in the three WHI ARs, as each crossed the central solar disk. Large values of  $R$  have been associated with flare activity.

1998), shown to increase magnetic free energy in some circumstances (Welsch, 2006), and proposed as a CME initiation mechanism (see, *e.g.*, Linker *et al.*, 2003), we tracked downhill features in magnetogram sequences of the WHI ARs, to investigate cancellation rates in each AR.

Using the YAFTA feature-tracking code (Welsch and Longcope, 2003; DeForest *et al.*, 2007; software and documentation are online at <http://solarmuri.ssl.berkeley.edu/~welsch/public/software/YAFTA/>) we only included pixels above 35 G (a  $2.5\sigma$  threshold) in features, and required each feature to have at least four pixels, and at least one 70 G pixel (a  $5\sigma$  peak threshold). We also required features to either persist for at least four frames, or interact with (fragment from, or merge with) a feature that persisted for four frames. The outlines of features identified in two successive magnetograms from AR 10987 are plotted over grayscale images of the magnetic field in Figure 6. The outlines are color coded by feature label, and features have been matched between these magnetograms. Different-color outlines imply distinct features were identified; same-color outlines generally imply matching features between frames, although the color palette used is limited, so spurious color matches are possible. While substantial evolution has occurred over the 96 minutes between these magnetograms, 90% of features in the first magnetogram were identified in the second, which is a typical survival rate.

Having tracked the three ARs' magnetogram sequences, we then attempted to quantify canceling features in each. We first found opposite-polarity features in close proximity by looping over positive features, applying IDL's dilate function, with a  $(3 \times 3)$  structuring



**Figure 6** The outlines of features – “hills” in absolute field strength – identified in two successive magnetograms from AR 10987 are plotted over grayscale images of the magnetic field (white is positive polarity, black negative; saturation is set at  $\pm 250$  G). The outlines are color coded by feature label, and features have been matched between these magnetograms. Different-color outlines imply distinct features were identified; same-color outlines generally imply matching features between frames.

element, to each feature’s pixels; and seeking instances of overlap between the dilated feature’s pixels and pixels of negative features. This essentially searched for negative features in nearest-neighbor pixels on the periphery of each positive feature. Hence, our definition of close proximity for defining cancellation is MDI’s pixel size,  $\approx 2'' \approx 1.4$  Mm. For a pair

**Table 4** Estimates of flux canceled in the WHI ARs, computed three ways (see text); canceled flux values are in units of  $[10^{20} \text{ Mx}]$ .

AR	# Events	# Multi-step	All events, $\sum \min(\delta\Phi)$	Multi-step, $\sum \text{avg}(\delta\Phi)$	Multi-step, $\sum \min(\delta\Phi)$
10987	58	10	5.0	4.0	1.9
10988	110	21	8.0	8.1	3.4
10989	42	5	2.9	1.6	0.8

of close features to have partially canceled over a time step, we further required the features' centers of flux to approach, and the flux of both features to decrease – and by doing so, we have implicitly assumed that neither feature disappears completely over a cancellation step.

This approach is subject to many sources of error. Thresholds imposed on field strengths in features imply that some magnetic flux is not included in any feature. Features' positions jitter, and their fluxes fluctuate, both from noise and true evolution. Furthermore, along the large-scale polarity-inversion lines where canceling features are typically identified, each feature often interacts with several neighboring like-polarity features, and possibly other opposite-polarity features, perhaps exchanging flux or canceling with those features, too. Hence, there are many essentially random sources of changes in features' fluxes and locations. With higher-cadence data, additional constraints might be imposed, *e.g.* meeting our cancellation criteria over several time steps. However, a more-detailed analysis of cancellation in higher-cadence data lies outside the purview of this study. Further, we are primarily interested in comparing canceled flux between the WHI ARs, not establishing absolute amounts of flux canceled.

Recognizing that our approach to quantifying canceled flux is subject to large uncertainties, we computed estimates in three ways: *i*) first, for each pair of canceling features identified, we took the *minimum* flux loss from the pair as the canceled flux in that event, and summed these fluxes from all cancellation events; *ii*) we limited our analysis to pairs of features that were observed to cancel over at least two steps, and took the *average* flux losses from such events; and *iii*) again restricting our attention to features that were observed to cancel over at least two steps, we summed the *minimum* flux lost from each pair in each event. The third approach is presumably the most restrictive method of estimating canceled flux.

For each AR, our tabulation of the total number of cancellation events, the number of multi-step cancellation events, and estimates for canceled flux are listed in Table 4. Variations between the estimates for a single AR provide a measure of the uncertainties, although as noted above, the method used for the third estimate is the most restrictive. If our identification of canceling features was essentially random, and mean feature fluxes in all three ARs were the same, then our estimates of cancellation events and canceled fluxes would follow the ratio of unsigned magnetic fluxes in the ARs, 1.4:1.7:1 (see Section 3.1 above). While the numbers in each column do follow the ordering of these ratios, there is an excess of both cancellation events and canceled flux in AR 10988 beyond that expected from variations in AR flux alone.

As with both total unsigned flux and unsigned flux  $[R]$  near SPILs, our analysis of flux cancellation in the WHI ARs suggests that AR 10988 should have been the most active, and AR 10989 the least.

### 3.3. Pixel-Scale Evolution

#### 3.3.1. Estimating Velocities

According to Faraday’s law, evolution of the radial magnetic field at the photosphere is governed by the curl of the electric field there:

$$\partial_t B_r = -c(\nabla \times \mathbf{E})_r. \tag{1}$$

Assuming that the electric field is ideal (equivalently, that the plasma’s conductivity is infinite) implies  $\mathbf{E} = -(\mathbf{v} \times \mathbf{B})/c$ , so evolution of the radial magnetic field can be related to horizontal variations in the velocity and magnetic fields by the ideal induction equation,

$$\partial_t B_r = \left[ \nabla \times (\mathbf{v} \times \mathbf{B}) \right]_r \tag{2}$$

$$= -\nabla_h \cdot (\mathbf{v}_h B_r - v_r \mathbf{B}_h). \tag{3}$$

The radial flux  $S_r$  of magnetic energy across the photosphere (the Poynting flux) depends upon  $\mathbf{E}$ , and in the ideal approximation on  $\mathbf{v}$ ,

$$S_r = c[\mathbf{E} \times \mathbf{B}]_r/4\pi = [v_r B_h^2 - (\mathbf{v}_h \cdot \mathbf{B}_h)B_r]/4\pi, \tag{4}$$

as does the rate of change of relative magnetic helicity (Berger and Field, 1984) in the corona  $[dH/dt]$  due to the helicity flux across the photosphere,

$$\frac{dH}{dt} = 2 \int dA [(\mathbf{A}_h^P \cdot \mathbf{B}_h)v_r - (\mathbf{A}_h^P \cdot \mathbf{v}_h)B_r], \tag{5}$$

where: the integration runs over the photosphere in the region of non-zero  $\mathbf{v}$  and  $\mathbf{B}$ ;  $\mathbf{A}^P$  is the vector potential of the current-free (and therefore curl-free, or “potential”) magnetic field  $\mathbf{B}^P$  that matches the observed photospheric radial field  $[B_r]$  *i.e.*  $\nabla_h \times \mathbf{A}_h^P = B_r^P$ , and  $A_r^P = 0 = \nabla_h \cdot \mathbf{A}_h^P$ .

Démoulin and Berger (2003) argued that the “footpoints” of magnetic fields anchored in the photosphere appear to move in magnetograms with an apparent footpoint velocity  $[\mathbf{u}]$ , which is related to the plasma velocity  $[\mathbf{v}]$  by

$$\mathbf{u} \equiv \mathbf{v}_h - (v_r/B_r)\mathbf{B}_h. \tag{6}$$

They further argued that tracking methods applied to magnetograms, such as local correlation tracking (*e.g.* Chae, 2001), would estimate  $\mathbf{u}$ , not  $\mathbf{v}_h$ . Welsch (2006) referred to  $\mathbf{u}$  as the flux transport velocity;  $\mathbf{u}B_r$  has units of a flux-transport rate (maxwells per unit length per unit time). Note that Equation (6) is a matter of definition, and so is made without approximation. In terms of  $\mathbf{u}$ , Equation (3) can be written in a form analogous to the continuity equation,

$$\partial_t B_r + \nabla \cdot (\mathbf{u}B_r) = 0. \tag{7}$$

The statement that tracking methods will accurately estimate  $\mathbf{u}$ , however, is a testable assertion; Schuck (2008) argued, in fact, that some “optical-flow” methods are relatively insensitive to radial flows, so will return a biased estimate  $\tilde{\mathbf{u}}$  of the true  $\mathbf{u}$ . Tests of several velocity-estimation methods conducted by Welsch *et al.* (2007) using synthetic data from MHD simulations, in which the true velocities were known, demonstrated that such methods

were far from perfect, but that their flow estimates were highly correlated with the true flows.

In terms of the flux-transport velocity, the Poynting and helicity fluxes in Equations (4) and (5) become

$$S_r = -(\mathbf{B}_h \cdot \mathbf{u}_h) B_r / 4\pi \quad (8)$$

$$\frac{dH}{dt} = -2 \int dA (\mathbf{A}_h^P \cdot \mathbf{u}_i) B_r. \quad (9)$$

Note that estimating the Poynting flux requires knowledge of the horizontal magnetic field.

The flux-transport velocity can be estimated from magnetogram sequences, with finite cadence  $\Delta t$  and pixel size  $\Delta x$ , by applying a finite-difference approximation to Equation (3):

$$\frac{\Delta B_z}{\Delta t} + \frac{\mathbf{\Delta} \cdot (\mathbf{u} B_r)}{\Delta x} = 0, \quad (10)$$

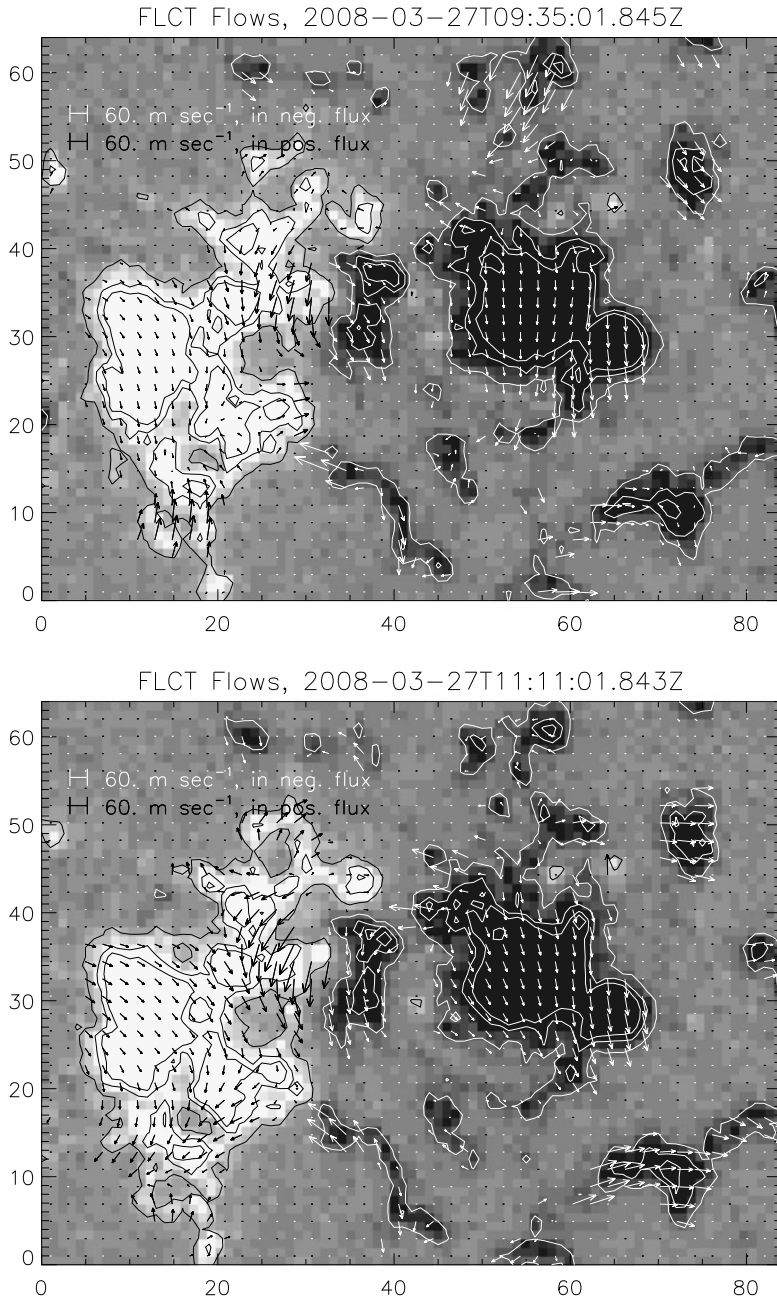
where  $\mathbf{\Delta}$  is the spatial finite-difference operator. If a typical flow speed is  $v_0$ , then the pixel-crossing time is  $\tau_0 = v_0 \Delta x$ . If  $\Delta t < \tau_0$ , then Equation (10) approximates Equation (7); if, however,  $\Delta t > \tau_0$ , the approximation can fail. This is analogous to the Courant–Friedrichs–Lewy (CFL) condition required for numerical stability in computational fluid dynamics.

Welsch *et al.* (2009) used Equation (10) as the basis for applying two tracking methods: Fourier local correlation tracking (FLCT: Welsch *et al.*, 2004; Fisher and Welsch, 2008) and the differential affine velocity estimator (DAVE: Schuck, 2006), to sequences of 96-minute MDI full-disk magnetograms (similar to the current data, but Level 1.8.0 instead of Level 1.8.2). Both methods employed similar windowing parameters (eight and nine pixels for FLCT and DAVE, respectively) to localize the magnetic data used in estimating the flow at a given pixel, which probably has the effect of averaging over smaller-scale flows. Correlation coefficients between the field-weighted FLCT and DAVE flows'  $x$ - and  $y$ -components were  $> 0.7$  over the set of all the flows computed by Welsch *et al.* (2009), implying consistency between flow estimates using distinct methods. Mean and median speeds for FLCT were  $\approx 65 \text{ m s}^{-1}$ , and for DAVE were  $\approx 105 \text{ m s}^{-1}$ ; evidently, DAVE speeds are higher than those estimated with FLCT. Given the  $\approx 1.4 \text{ Mm}$  disk-center width of MDI full-disk pixels, these speeds imply pixel-crossing times of  $\approx 4\text{--}6 \text{ hr}$ . Welsch *et al.* (2009) also found that flow directions remained significantly correlated over similar time scales. Both of these facts imply that 96-minute cadence, full-disk MDI data can be used with Equation (10) as a valid approximation of Equation (7).

We applied FLCT to the 96-minute cadence MDI full-disk magnetograms within 23 March 2008, 00:00:00 UT–4 April 2008, 00:00:00 UT from the WHI interval, with a windowing parameter of eight pixels, an absolute field-strength threshold for tracking of 50 G, and a low-pass spatial wavenumber roll-off parameter of 0.25 (see Fisher and Welsch, 2008). Pixels out to  $45^\circ$  from disk center were tracked. This choice of windowing parameter corresponds to  $\approx 10 \text{ Mm}$ , a scale much larger than granules, but slightly smaller than supergranules (Hagenaar, Schrijver, and Title, 1997).

Data cubes covering each of the WHI ARs' magnetic fields and their corresponding flows were then extracted from the full-disk magnetograms and inner-disk flow maps for the time intervals listed in the bottom three rows of Table 3. Figure 7 shows two successive FLCT flow maps from the central, strong-field portion of AR 10987, from the same magnetograms shown in Figure 6. Some evolution in the flow pattern can be seen over the 96 min-





**Figure 7** Two successive FLCT flow maps from the central, strong-field portion of AR 10987, from the same magnetograms shown in Figure 6. Background grayscale shows estimated radial field strength, white showing positive flux, black negative, with saturation set at  $\pm 250$  G. White/black contours correspond to  $\pm 100$ ,  $\pm 300$ , and  $\pm 500$  G. For clarity, only every other flow vector is plotted. Some evolution in the flow pattern can be seen; but flows in many regions appear generally similar at both times.

utes between the flow maps; but flows in many regions appear qualitatively similar at both times.

### 3.3.2. Proxy Poynting Flux

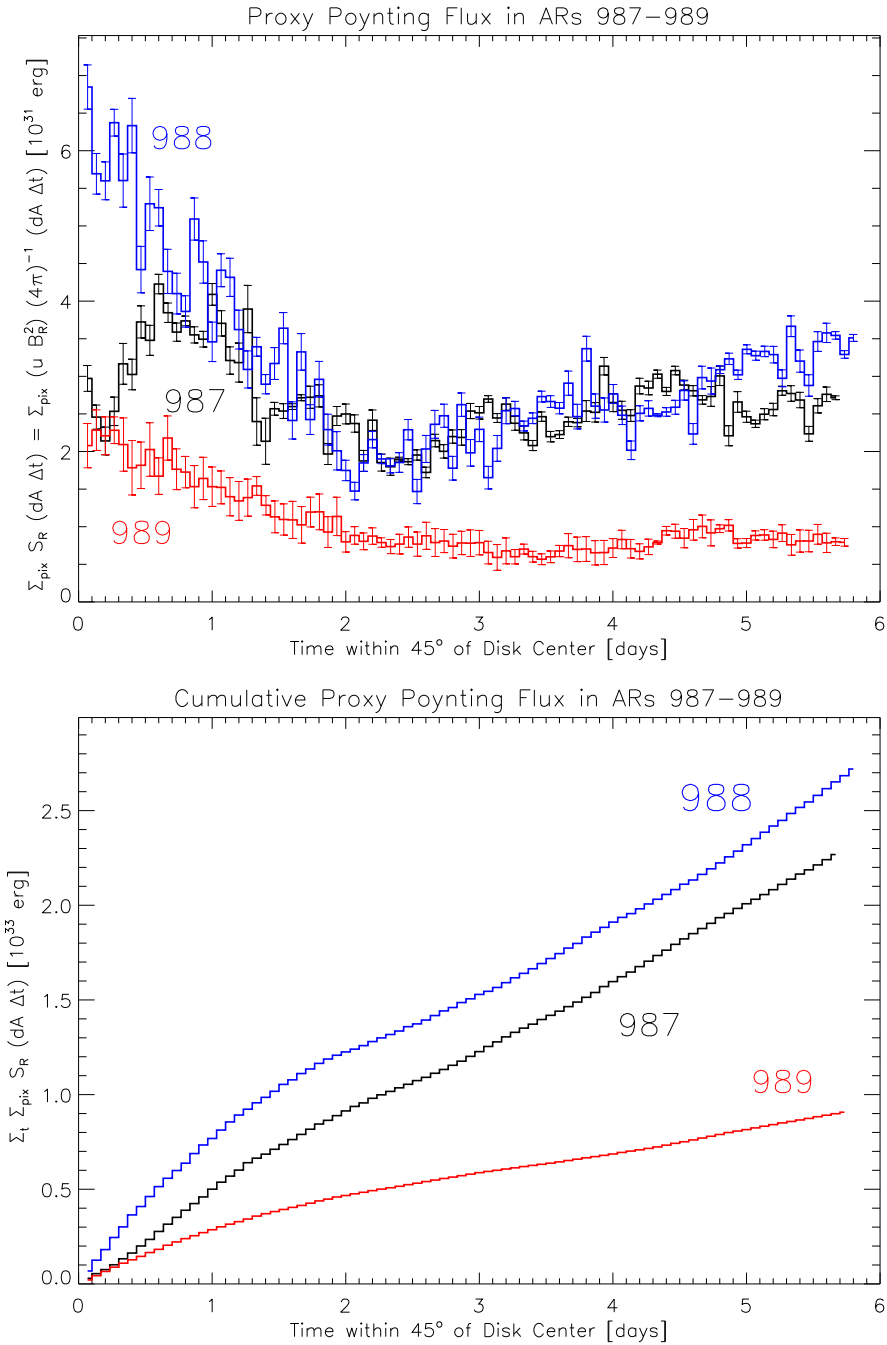
Welsch *et al.* (2009) analyzed relationships of flare activity with photospheric magnetic field and flow properties in a sample of a few dozen ARs. Of several quantities that they investigated, they found Schrijver's  $R$ -value and a quantity proportional to  $\sum(uB_R^2)$ , where  $u = |\mathbf{u}|$ , and the sum runs over the AR magnetograms, to be most strongly associated with flare activity. Because  $uB_R^2$  has the same dimensions as the Poynting flux of magnetic energy [ $\text{erg cm}^{-2} \text{s}^{-1}$ ], Welsch *et al.* (2009) called this quantity the proxy Poynting flux. For consistency with Equation (8), we define the proxy Poynting flux here to be  $S_R \equiv (uB_R^2)/4\pi$ . (Note that this definition differs from that of Welsch *et al.* (2009), who defined  $S_R$  to include a sum over pixels – a total flux, instead of a flux density – and did not include  $4\pi$ .) Li *et al.* (2010) estimated the proxy Poynting flux in AR 8038 around the time of the well-known 12 May 1997 flare/CME, and found the cumulative flux reached  $\approx 10^{32}$  erg over the four-day interval before the eruption.

What is the physical basis for the relationship between the proxy Poynting flux and flare activity? Leaving aside the likelihood that estimates of  $B_r$  and  $\mathbf{u}$  are imperfect, in principle,  $S_R$  corresponds to part of the horizontal Poynting flux [ $S_h$ ] (additional contributions arise from terms containing  $\mathbf{B}_h$ ). The magnetic energy that powers flares and CMEs enters the corona from the solar interior, as an outward, radial Poynting flux [ $S_r$ ]. It is plausible that there should be a correlation between  $S_r$  and flare/CME activity, although the corona can store magnetic energy, so there might typically be a latency between the introduction of magnetic energy into the corona and its release in flares/CMEs. For instance, Longcope *et al.* (2005) and Schrijver *et al.* (2005) report latency times associated with active-region magnetic fields of  $\approx 24$  hours. (And in quiet-Sun regions, filaments/prominences, which are interpreted as current-carrying [non-potential] magnetic field structures, can persist in the corona for weeks.) It is also plausible that the radial Poynting flux [ $S_r$ ] is significantly correlated with [ $S_h$ ] and/or the proxy flux [ $S_R$ ], but no quantitative theoretical or observational characterization of such a correlation has been presented.

Using the FLCT flows we estimated for each WHI AR, we computed the proxy Poynting flux in that AR over the time interval between each tracked magnetogram pair. We then multiplied by (reprojection-corrected) pixel area [ $\Delta A$ ] and the time interval [ $\Delta t$ ] between magnetograms, and summed over all pixels to express our results in terms of ergs of energy transported. Results are plotted in the top panel of Figure 8; in the bottom panel, we plot the cumulative proxy Poynting fluxes over time. As with  $R$ , we estimated uncertainties in the top panel from a running-boxcar computation of the standard error in the mean. Assuming a combined fractional uncertainty of 0.6 for the terms in the product  $uB_R^2$  in each pixel resulted in error bars smaller than those shown. Summing the uncertainties in the top panel in quadrature for the cumulative result shown in the bottom panel yields error bars about the size of the steps in the bottom panel.

Unlike the true Poynting flux, which can be positive or negative (*i.e.* radially outward or inward), the proxy Poynting flux is only positive. To the extent that the proxy Poynting flux reflects the outward radial flux of magnetic energy, the values in these plots suggest the order of magnitude of energy transport in the WHI ARs.

As with other magnetic parameters of the WHI ARs, values of the proxy Poynting flux suggest AR 10988 should have been the most active, and AR 10989 the least.



**Figure 8** The proxy Poynting flux [ $S_R$ ] multiplied by pixel area [ $\Delta A$ ] and the time between magnetograms [ $\Delta t$ ] (top) and its sum over time for the three WHI ARs, as each crossed the central solar disk. Error bars for the cumulative plot would be about as large as vertical step sizes. Large values of  $\sum_{\text{pix}} S_R$  have been associated with flare activity. The sum over  $S_R$  can provide an order-of-magnitude estimate of the magnetic-energy transport rates.

### 3.3.3. Helicity Flux

Magnetic helicity is approximately conserved even when magnetic reconnection occurs, meaning that it is not readily dissipated in the corona (Berger, 1984), and can accumulate there as twisted magnetic flux emerges from the interior (Pevtsov, Canfield, and McClymont, 1997). It is plausible that helicity accumulation in the corona plays a key role in triggering CMEs (Low, 2001).

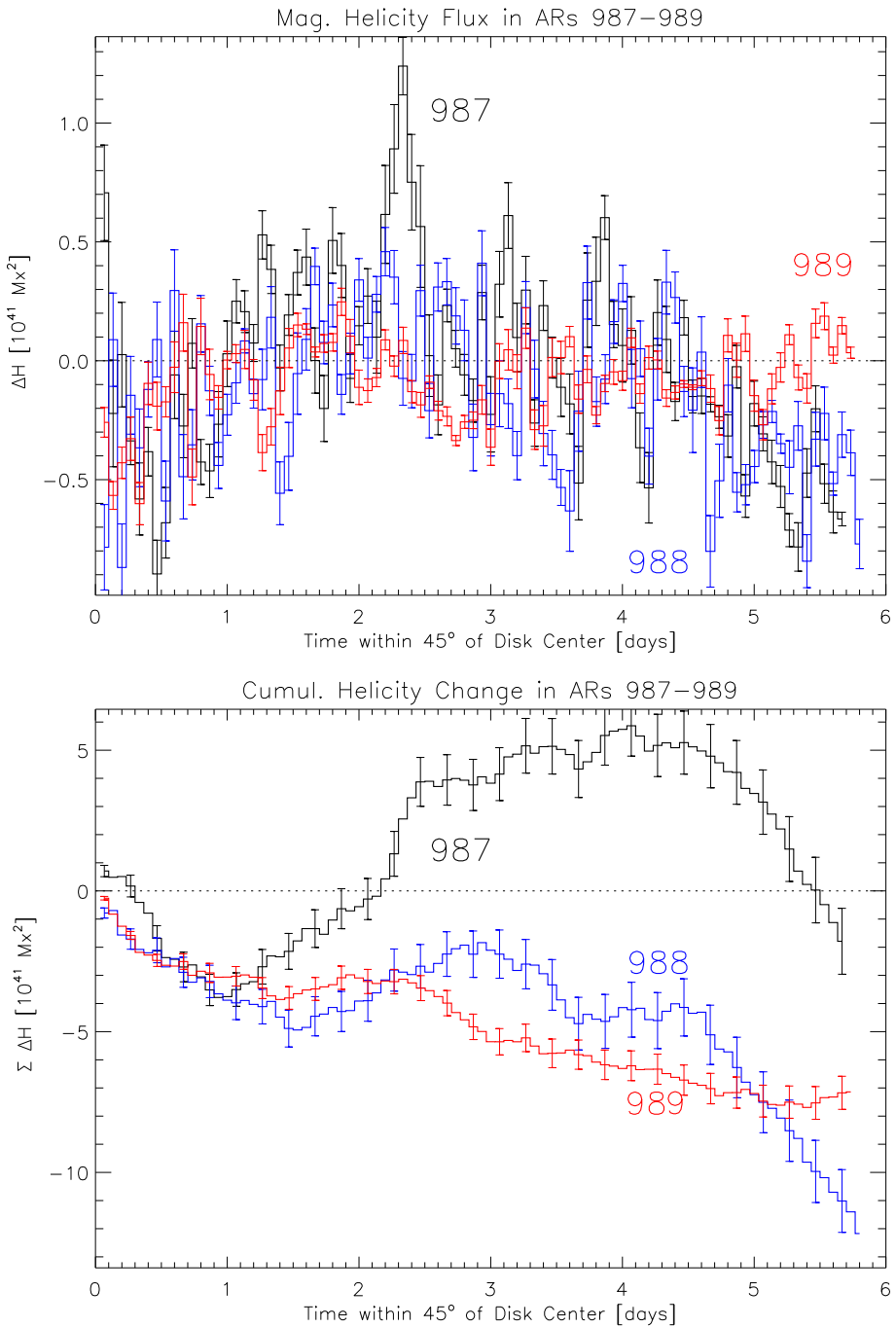
Velocities inferred from tracking can also be used to estimate the flux of magnetic helicity across the photosphere (*e.g.*, Chae, 2001; Kusano *et al.*, 2002; Pariat, Demoulin, and Berger, 2005). Using the FLCT flows we estimated for each WHI AR, we computed the helicity flux in that AR over the time interval between each tracked magnetogram pair, separately using *i*) Equation (9) with a Green's function method to calculate  $A^P$ , and *ii*) the method presented by Pariat, Démoulin, and Berger (2005). Means, medians, and linear fits between the two methods agreed to within 3% for AR 10987, 1% for AR 10988, and 6% for AR 10989. In the top panel of Figure 9, we show the differential fluxes of helicity for the WHI ARs computed from Equation (9), with uncertainties again computed from a running-boxcar calculation of the standard error in flux estimates. (As above, formally propagated errors were too small to appear on these plots.) In the lower panel of Figure 9 we plot the cumulative helicity fluxes of each WHI AR; only every third error bar is plotted, for clarity.

A characteristic magnitude for helicity is the flux in the system squared. In Figure 10, we plot the cumulative helicity fluxes of each WHI AR, normalized by the square of the mean magnetic flux in each AR over the time period it was observed. The unnormalized, cumulative, helicity fluxes for ARs 10988 and 10989 are similar; but since the relative magnetic fluxes of the ARs 10987, 10988, and 10989 are 1.4:1.7:1, normalizing by their squared fluxes implies the characteristic helicity for AR 10989 is substantially higher than for 10988.

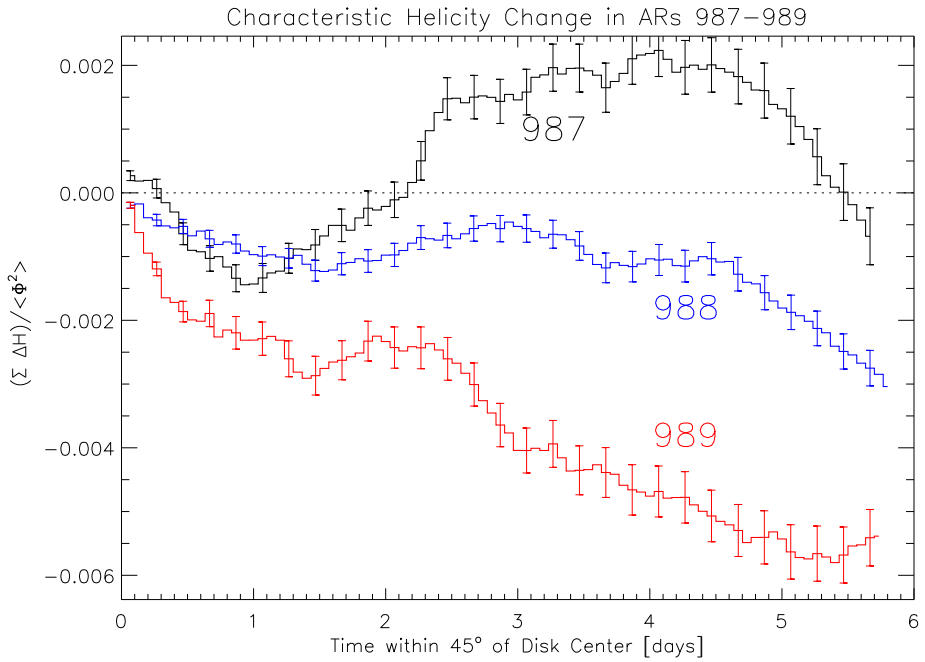
We have reviewed several magnetic parameters of the WHI ARs that might be correlated with flare and CME activity. Characteristic helicity is the only such parameter for which AR 10989 has a larger value than the other ARs. The characteristic helicity fluxes that we found, however, are far below unity, implying that the helicity fluxes did not inject large amounts of twist into the WHI ARs, relative to their magnetic size.

The total helicity present in an AR is the combination of that present in the AR when it emerged and the helicity injected after emergence. By extrapolating non-linear force-free fields (NLFFFs) from a vector magnetogram, the instantaneous helicity content of an AR can be estimated. Petrie, Canou, and Amari (2011) have done this for the WHI ARs with SOLIS (Henney *et al.*, 2009) data, and report characteristic helicities (see their Table 1) of 0.0055, 0.0041, and 0.0017 for ARs 10987, 10988, 10989, respectively. Note that all of their characteristic helicity values are of the same order as those we report, but that all of their values are positive; and that their value of the characteristic helicity in AR 10989 is less than those of the other WHI ARs, undermining the hypothesis that characteristic helicity might explain variations in flare and CME productivity.

As an aside, we note that some of our estimates of helicity *changes* also differ from those of Petrie, Canou, and Amari (2011) (see the right column of their Figure 23). They show AR 10987 with initially positive helicity that tends to decrease with time, which only partially agrees with our results, which show an initially negative helicity flux followed by a larger, positive helicity flux. Our estimates show negative helicity steadily being added to AR 10988 over time, but Petrie, Canou, and Amari (2011) found increasingly positive helicity over one time interval. Finally, the estimates of helicity changes in AR 10989 by Petrie, Canou, and Amari (2011) are relatively weak, and of mixed sign; but our results show a steady flux of negative helicity.



**Figure 9** Top: the differential fluxes of helicity for the WHI ARs, with uncertainties. Bottom: The cumulative helicity fluxes of each WHI AR; only every third error bar is plotted, for clarity.



**Figure 10** The cumulative characteristic helicity fluxes of each WHI AR: the cumulative helicity flux, normalized by the square of the mean magnetic flux in each AR over the time period it was observed. The unnormalized, cumulative, helicity fluxes for ARs 10988 and 10989 are similar, but the characteristic helicity for AR 10989 is substantially higher than for 10988.

### 3.4. Inductive Flow Estimation

Flows can be estimated from the induction equation alone, by first applying a Helmholtz decomposition to the horizontal electric field,

$$c\mathbf{E}_h = -\nabla_h\phi + \nabla_h \times \chi \hat{\mathbf{r}}, \tag{11}$$

and using this result in Equation (1), resulting in a Poisson’s equation for  $\chi$ ,

$$\partial_t B_r = \nabla_h^2 \chi. \tag{12}$$

If the electric field is assumed to be ideal, then  $c\mathbf{E}_h = -\mathbf{u} \times B_r \hat{\mathbf{r}}$ , and a “Poisson flow” can be derived from  $\chi$ ,

$$\mathbf{u} B_r = -\nabla_h \chi. \tag{13}$$

We solved the finite-difference approximation to Equation (12) for the WHI AR magnetogram sequences using Fast Fourier Transforms (FFTs), and then derived Poisson flows. Mean and median Poisson-flow speeds for the pair of magnetograms shown in Figure 7 were 91 and 63  $\text{m s}^{-1}$ , respectively, slow enough to be consistent with the finite-difference approximation.

One problem with this approach is that fluctuations in individual pixels due purely to noise or observational artifacts are ascribed to actual electric fields or flows. In contrast, tracking methods such as FLCT and DAVE estimate flows at a given pixel using data from

the neighborhood around that pixel (defined with windowing functions), and are therefore less susceptible to spurious fluctuations in field strengths in any individual pixel.

Attempts to ameliorate this shortcoming by smoothing the field difference  $[\Delta B_R]$  rapidly degraded the consistency of the Poisson solution with the actual magnetic evolution. This consistency is checked using Equation (7) to calculate the expected magnetic evolution assuming  $\mathbf{u}B_R$  is known (e.g. Welsch *et al.*, 2007). Temporal averaging of higher-cadence data, however, should counteract the effects of spurious, pixel-scale magnetic fluctuations, but still enable consistency between derived flows and Equation (7).

Unfortunately, statistical agreement between FLCT and Poisson-flow components is poor, with both linear and rank-order correlations below 0.1 for the magnetogram pair in Figure 7, both when weighted by  $B_R$  and not. Proxy Poynting fluxes derived from tracking and Poisson-flow estimates are significantly correlated, but this could arise solely from spatial correlation of  $B_R^2$ . Helicity fluxes derived from tracking and Poisson-flow estimates are also poorly correlated. Unlike the proxy Poynting flux, helicity-flux density depends sensitively upon *direction* of flow, since  $\mathbf{u}$  is dotted with  $\mathbf{A}^P$ . Given that FLCT and Poisson-flow components are weakly correlated, such disagreement in helicity fluxes is not surprising.

Given these disagreements between results from each method, which flow estimate is more credible? Welsch *et al.* (2009) found flow estimates from the FLCT and DAVE methods – both of which are optical-flow techniques, but derive flow estimates in very different ways (Schuck, 2006; Fisher and Welsch, 2008) – were significantly correlated. If weighted by  $B_R$ , linear correlation coefficients were  $> 0.7$  for each flow component for more than 2000 magnetogram pairs in their dataset. In addition, Welsch *et al.* (2009) found that flow components derived from either FLCT or DAVE persisted in time, with a decorrelation time of approximately six hours (see their Figures 9 and 10). In contrast, Poisson flows for AR 10987 have much lower frame-to-frame correlations than FLCT flows; they essentially decorrelate after one 96-minute interval. Both correlations between flows determined using the independent FLCT and DAVE methods and the persistence of FLCT and DAVE flows in time suggest that the FLCT results found here are more credible than the Poisson flows.

Welsch *et al.* (2007) tested several velocity-estimation methods using synthetic magnetogram sequences extracted from MHD simulations, in which the flows were known. Later, Welsch and Fisher (2008) tested Poisson-flow estimates with the same synthetic data, and found them to be about as accurate as optical-flow estimates. Since the tracking and Poisson flows were both significantly correlated with the known MHD flows, they were also significantly correlated with each other. The lack of agreement between FLCT and Poisson flows found here for 96-minute cadence, full-disk MDI magnetogram data suggests the Poisson method of estimating flows might fail when applied to such data. The Poisson technique might, however, fare better when applied to data with higher cadence and/or higher spatial resolution, such as data from either MDI in its high-resolution mode or HMI. Further study of Poisson-flow estimates is planned.

#### 4. Discussion

By all of the statistical predictors of flare activity based upon magnetogram structure and evolution that we investigated, AR 10989 should have been significantly less active than both AR 10987 and 10988. During the intervals that we tracked each AR, however, flare activity in AR 10989 was comparable to activity in the other ARs. Further, Webb *et al.* (2011) found AR 10989 to be much more CME productive than the other two ARs.

Why did these statistical predictors fail in the case of the WHI ARs? Given that we only consider three ARs here, and that these predictors are purely statistical, we should not be

too surprised that there are exceptions. Also, flares are rare events, and the time interval of our observations was limited, so drawing conclusions about activity levels from the small number of flares observed is problematic. While we only analyzed the ARs from the WHI for this study, stronger conclusions regarding relationships (or lack thereof) between ARs' photospheric magnetic properties and flares could presumably be made by studying a larger AR sample. Nonetheless, it would be useful if some physical basis for the exceptions we found could be identified.

Unfortunately, the observations available to us are of limited utility in this regard. First, a practical concern: as noted above, we have only LOS-magnetogram sequences for the WHI ARs. Long-duration, regular-cadence vector-magnetogram sequences (such as those available from HMI, or that might be available from a network of terrestrial, SOLIS-like instruments) can reveal much more about the structure and evolution of AR magnetic fields.

Second, another practical concern: we are largely ignorant of the WHI active regions' magnetic structure and coronal activity over much of their lives. A significant component of AR 10989's activity occurred both before and after we tracked it across the central solar disk. Because the structure and evolution of its photospheric magnetic field could only be reliably estimated while on the central disk, we can only speculate about this field away from disk center. Welsch *et al.* (2009) showed that AR magnetic fields can evolve substantially over the course of 24 hours, and Longcope *et al.* (2005) and Schrijver *et al.* (2005) estimated coronal energy storage times on the order of a day. If the field of AR 10989 evolved significantly between its time on the central disk and the pre- and post-tracking intervals, its photospheric magnetic structure during those more active intervals might have been more consistent with statistical expectations based upon its coronal activity level. Similarly, we often only have hints about flares and CMEs produced by ARs beyond the limb. For instance, STEREO-A data show that on 05 April, AR 10987 at longitude W105 produced a CME just before 16:00 UT with a speed estimated from LASCO data at  $962 \text{ km s}^{-1}$ , associated with an A-class GOES flare. (See Nitta's excellent compilation of data for this and other events at [http://www.lmsal.com/nitta/movies/flares\\_euvi/](http://www.lmsal.com/nitta/movies/flares_euvi/).) Burkepile *et al.* (2004) have shown that GOES flux is correlated with CME kinetic energy, with a linear correlation coefficient of 0.74. Similarly, the events analyzed by Qiu and Yurchyshyn (2005) show that GOES flux is correlated with CME speed: we find linear and rank-order correlation coefficients of 0.79 and 0.54, respectively, in their sample of 13 events. These results suggest that the A-class flare observed by GOES was most likely a partially occulted strong C-class or weak M-class flare. To address this ignorance, having more extensive magnetograph, X-ray, *in-situ*, and EUV coverage of the Sun would be useful. A satellite in co-rotation with the Sun could provide comprehensive observations of ARs from birth to death; and a constellation of satellites might provide full, " $4\pi$ " coverage.

Third, studying photospheric data alone neglects aspects of coronal magnetic structure that are relevant to flaring. For instance, the large-scale structure of the coronal magnetic field, including perhaps the proximity of an AR to open magnetic fields, might play a key role in CME productivity. Sterling and Moore (2001) argued that open flux near NOAA AR 8210 enabled repeated, homologous ejections (see their Figure 3). Similarly, Liu (2007) reported that CMEs underneath the streamer belt tended to be substantially slower than CMEs outside the belt, suggesting that the global magnetic environment around ARs can play a significant role in the CME process. Global-scale potential-field source–surface (PFSS) modeling by Petrie, Canou, and Amari (2011) demonstrates that AR 10989 lies almost completely outside the streamer belt (see their Figure 21), perhaps easing the ejection of coronal fields into the heliosphere as CMEs. Differences in large-scale coronal magnetic environment might partially explain why flare activity levels were broadly similar among the WHI



ARs, but CME activity levels were not. (It is also true that flares and CMEs appear to be distinct phenomena: very large flares are almost always associated with CMEs, but that the association is weaker with weaker flares (Andrews, 2003).) It would be useful to study objective, quantitative measures of “proximity” between open flux and ARs, and correlations between CME activity and such proximity measures. Hudson and Li (2010) noted that the flare-to-CME ratio increased this solar minimum relative to the last, implying the corona “was relatively easy to disrupt” during this minimum, also suggesting global properties of the coronal magnetic field might play some role in the CME process.

Fourth, properties of photospheric magnetic fields might be essentially unrelated to properties of the coronal magnetic field that actually generate flares and CMEs. Having analyzed a large sample of vector magnetograms, Leka and Barnes (2007) suggested “the state of the photospheric magnetic field at any given time has limited bearing on whether that region will be flare productive.” (Based upon the case studies here, we might add the evolution of the line-of-sight photospheric magnetic field over any given time interval also has limited bearing on whether that region will be flare productive – but we have not analyzed enough cases to justify such a conclusion.) Efforts to measure properties of coronal magnetic fields using IR (SOLARC: Lin, Kuhn, and Coulter, 2004; CoMP: Tomczyk and McIntosh, 2009; ATST: Cargill, 2009) and radio (FASR: Cargill, 2009) instruments could lead to breakthroughs in our understanding of flare and CME physics.

Finally, leaving aside all observational limitations, flares might be unpredictable for more fundamental reasons, a possibility also noted by Schrijver (2009).

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