



University | School of Physics  
of Glasgow & Astronomy

# SUPA course: The Sun's Atmosphere

Session 2021-22

Lecture 10 on “Observing and interpreting solar magnetism”

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## The course thus far :

- 10/01/2022 Lecture 1: Introduction (Labrosse)
- 11/01/2022 Lecture 2: Solar atmosphere (Labrosse)
- 17/01/2022 Lecture 3: Plasma physics 1 (Kontar)
- 17/01/2022 Lecture 4: Plasma physics 3 (Kontar)
- 24/01/2022 Lecture 5: MHD 1 (MacTaggart)
- 25/01/2022 Lecture 6: MHD 2 (MacTaggart)
- 01/02/2022 Lecture 8: Radiation transport (Labrosse)
- 07/02/2022 Lecture 9: The solar photosphere (Hudson)
- 08/02/2022 **Lecture 10: Solar magnetism (Hudson)**

# Useful homework questions based on this material

- Can one detect an oscillating coronal loop by Doppler shifts?
- For what value of  $B$  can a flux tube escape from the tachocline and emerge in one cycle?
- What is the electrical potential at the photosphere?
- At what stereoscopic angle can Stokes (I,V) do better than Stokes (I,Q,U,V)?

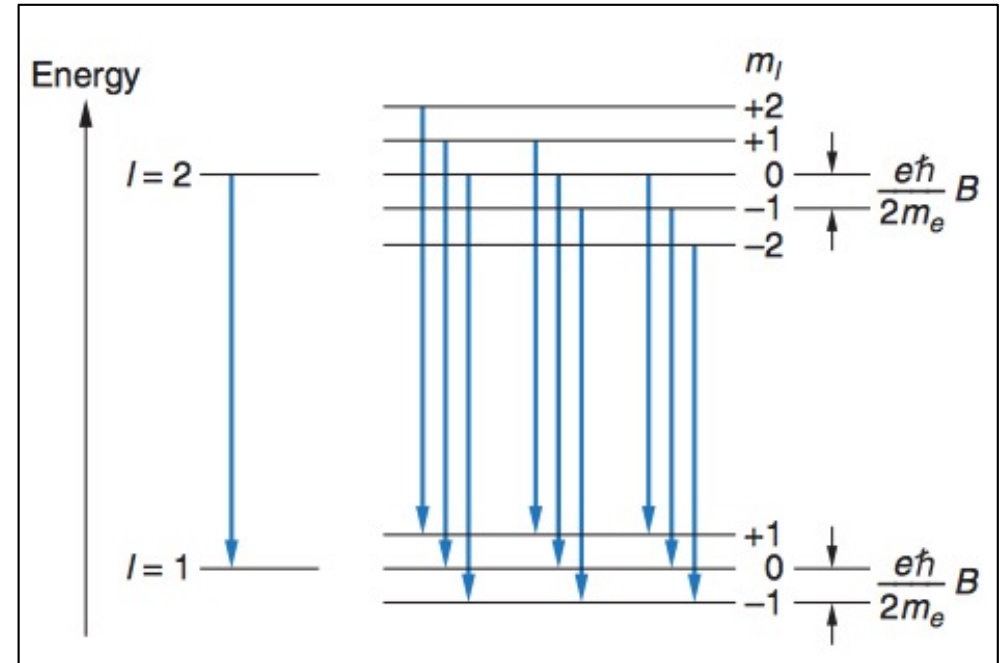
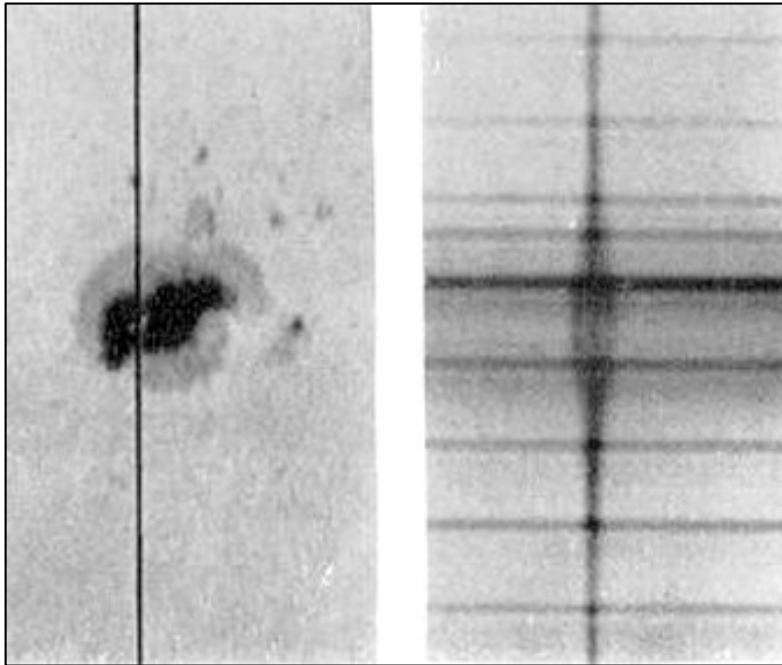
*These are questions to be answered by rough approximation, and the necessary facts should be here on the slides. I will post discussion of these items on Files and at*

*<http://www.ssl.berkeley.edu/~hudson/presentations/supa.220207/>*

# Sunspots and faculae are magnetic in nature

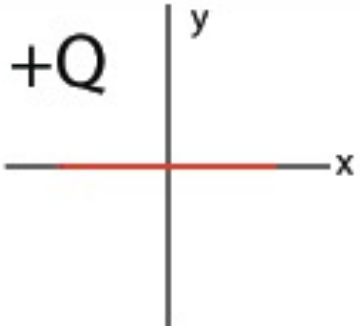
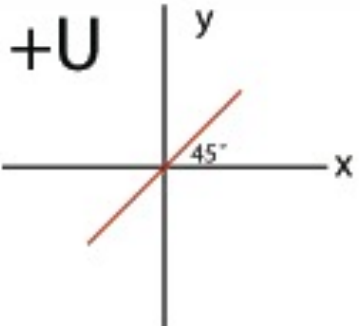
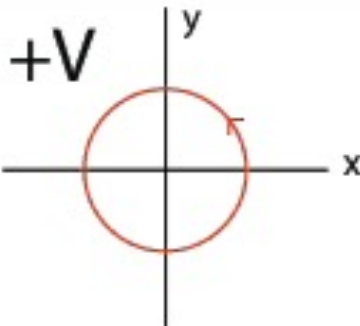
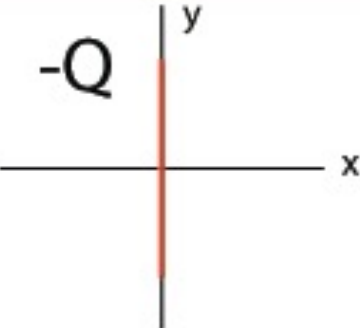
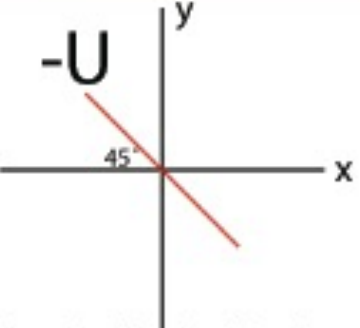
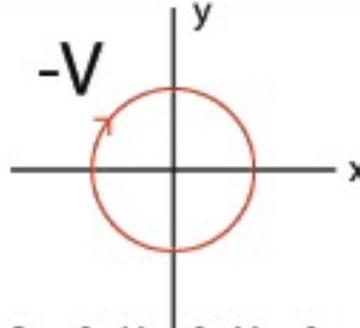
- The *spectrohelioscope*, invented in the 19<sup>th</sup> century, enabled monochromatic views, for example in H $\alpha$ .
- The measurement of circular polarization enabled Hale to recognize Zeeman splitting in sunspot umbrae, confirming the hint given by vortex-like patterns of H $\alpha$  fibrils.
- As reported by Jurčák et al. (2018) an umbra forms wherever  $B_z > 0.14$  T (a fridge magnet!)

# The Zeeman effect



- Magnetic fields distort atomic energy levels in a polarized manner.
- For sunspot 0.1 T fields, the splitting is visible to the naked eye in a spectroscope. The “Bohr Magneton” is  $5.788 \times 10^{-5}$  eV/T.
- The splitting depends upon the angle  $\langle B, \text{eye} \rangle$ : the  $\sigma$  components (linear polarization) reflect the perpendicular field, whereas the  $\pi$  components (circular) reflect the line-of-sight field.

# Three of the Stokes parameters

100% Q	100% U	100% V
<p><b>+Q</b></p>  <p><math>Q &gt; 0; U = 0; V = 0</math></p> <p>(a)</p>	<p><b>+U</b></p>  <p><math>Q = 0; U &gt; 0; V = 0</math></p> <p>(c)</p>	<p><b>+V</b></p>  <p><math>Q = 0; U = 0; V &gt; 0</math></p> <p>(e)</p>
<p><b>-Q</b></p>  <p><math>Q &lt; 0; U = 0; V = 0</math></p> <p>(b)</p>	<p><b>-U</b></p>  <p><math>Q = 0; U &lt; 0; V = 0</math></p> <p>(d)</p>	<p><b>-V</b></p>  <p><math>Q = 0; U = 0; V &lt; 0</math></p> <p>(f)</p>

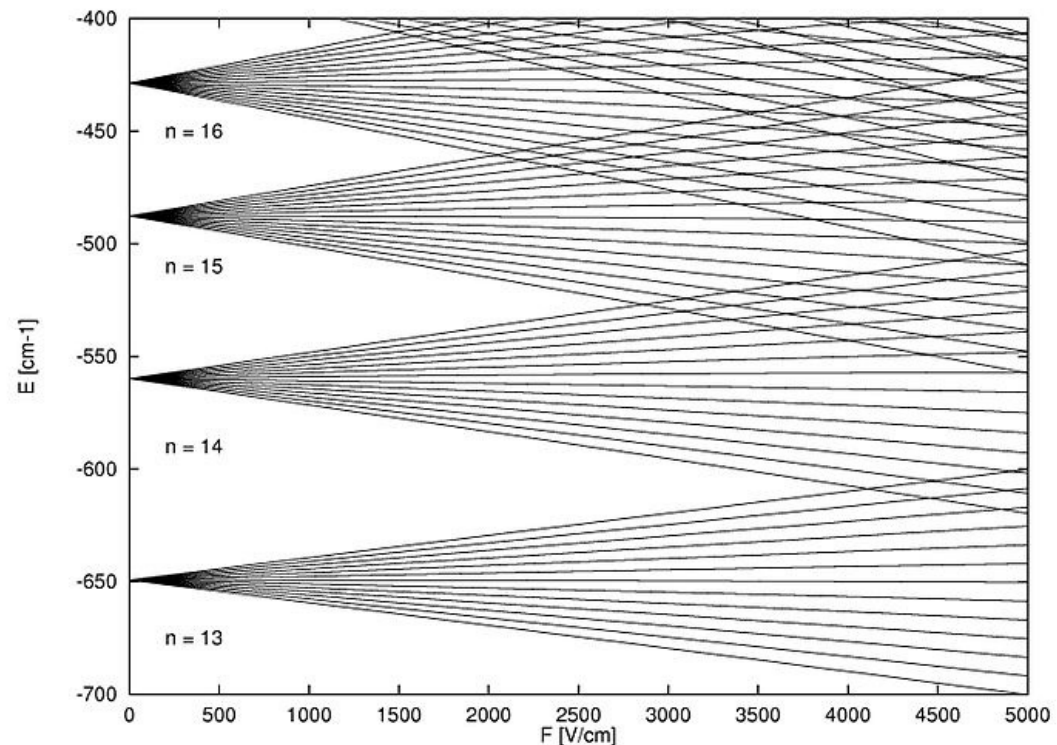
(the fourth Stokes parameter is just the intensity I)

# Other observations of B

- **The Hanle effect** results from line depolarization when the collision frequency exceeds the Larmor frequency.
- **Faraday rotation** alters the polarization angle of a linearly polarized background source (e.g., a quasar).
- **Image striations** can be interpreted in terms of field direction: note that would be  $\sim 2/3$  of the problem of measuring  $\mathbf{B}(\mathbf{r})$ .
- **Gyrosynchrotron** radiation has natural circular polarization.
- **Birefringence effects** polarize even thermal emission from magnetized plasmas.

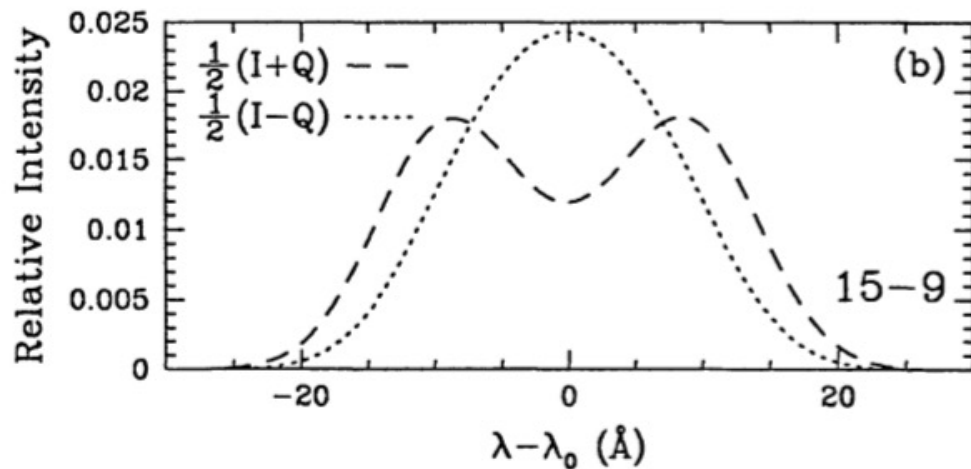
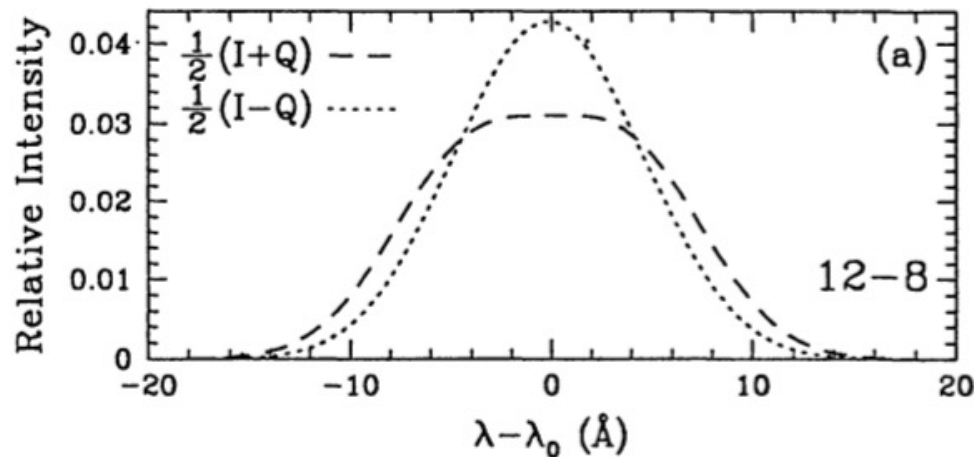
# E observations

- **The Stark effect** results from level shifts due to the presence of an electric field (the generic term).
- **Pressure broadening** is the Stark effect at the atomic level in a dense plasma.





# Stark Effect



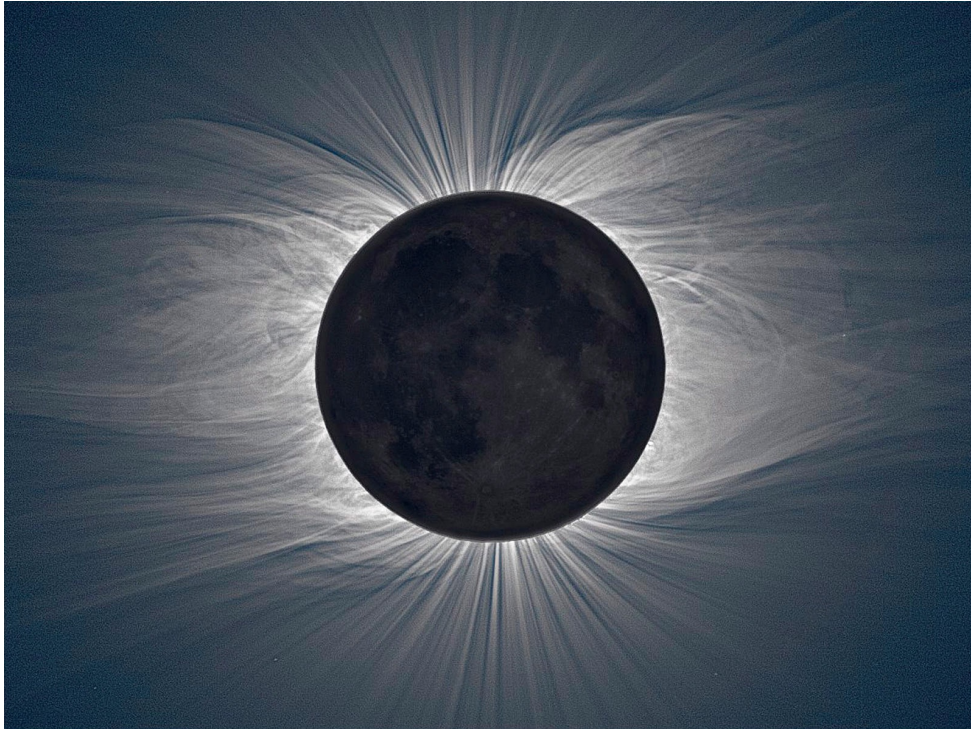
- The effect is strongest for “Rydberg” states (e.g.,  $n = 20$ ), hence ALMA?
- Minimum detectable macroscopic fields may be of order 100 V/m.

# Data cubes

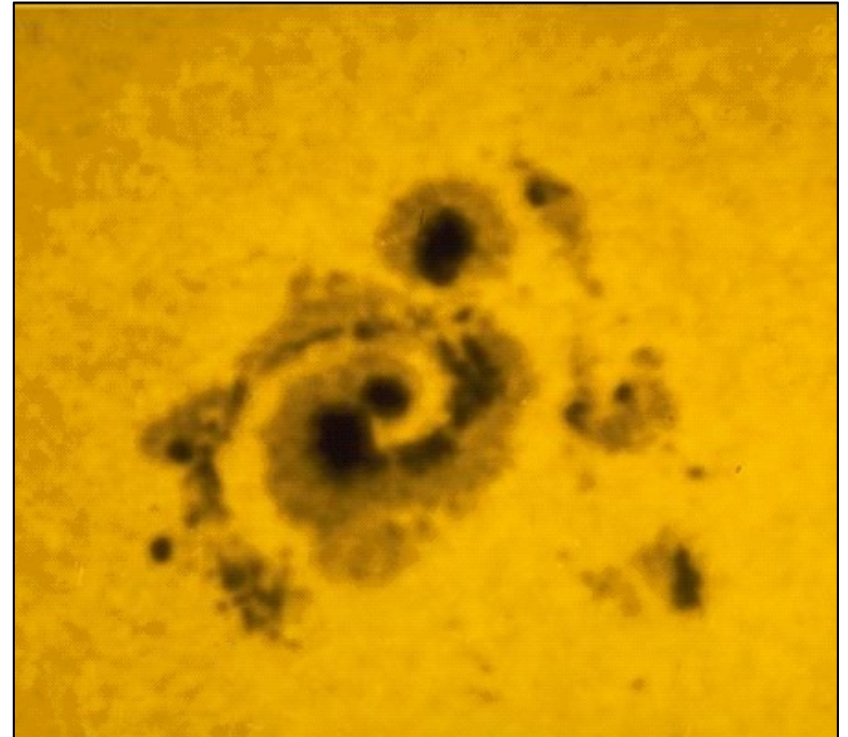
- The measurement process yields fluxes and errors:  $f(x,y,\lambda,p,t)$  and  $\delta f(x,y,\lambda,p,t)$ .
- In principle the four Stokes parameters must be measured, with attendant problems in radiative-transfer theory; to get I, Q, U, V means four independent spectra are needed at each pixel and time:  $f(\lambda,p)$  with  $p = [I,Q,U,V]$
- Observational caveats: line-of-sight confusion and differing heights of formation of each parameter.

The bottom line might be (4096,4096,1e5,4,1e5) for one hour's data: 1 EB (exabyte).

# Solar magnetism



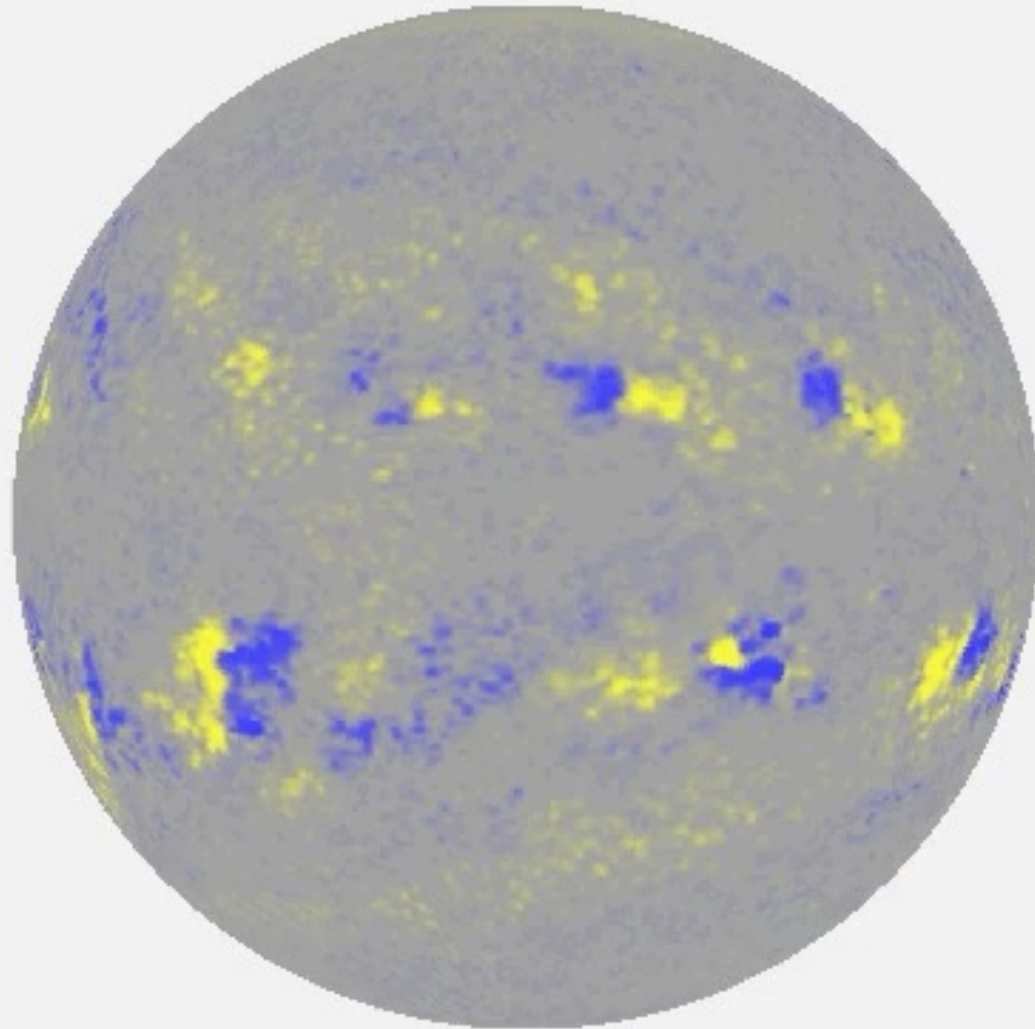
- The fine striations at the poles during an eclipse sure look like a dipole magnetic field.



- Sometimes sunspots have spiral patterns.

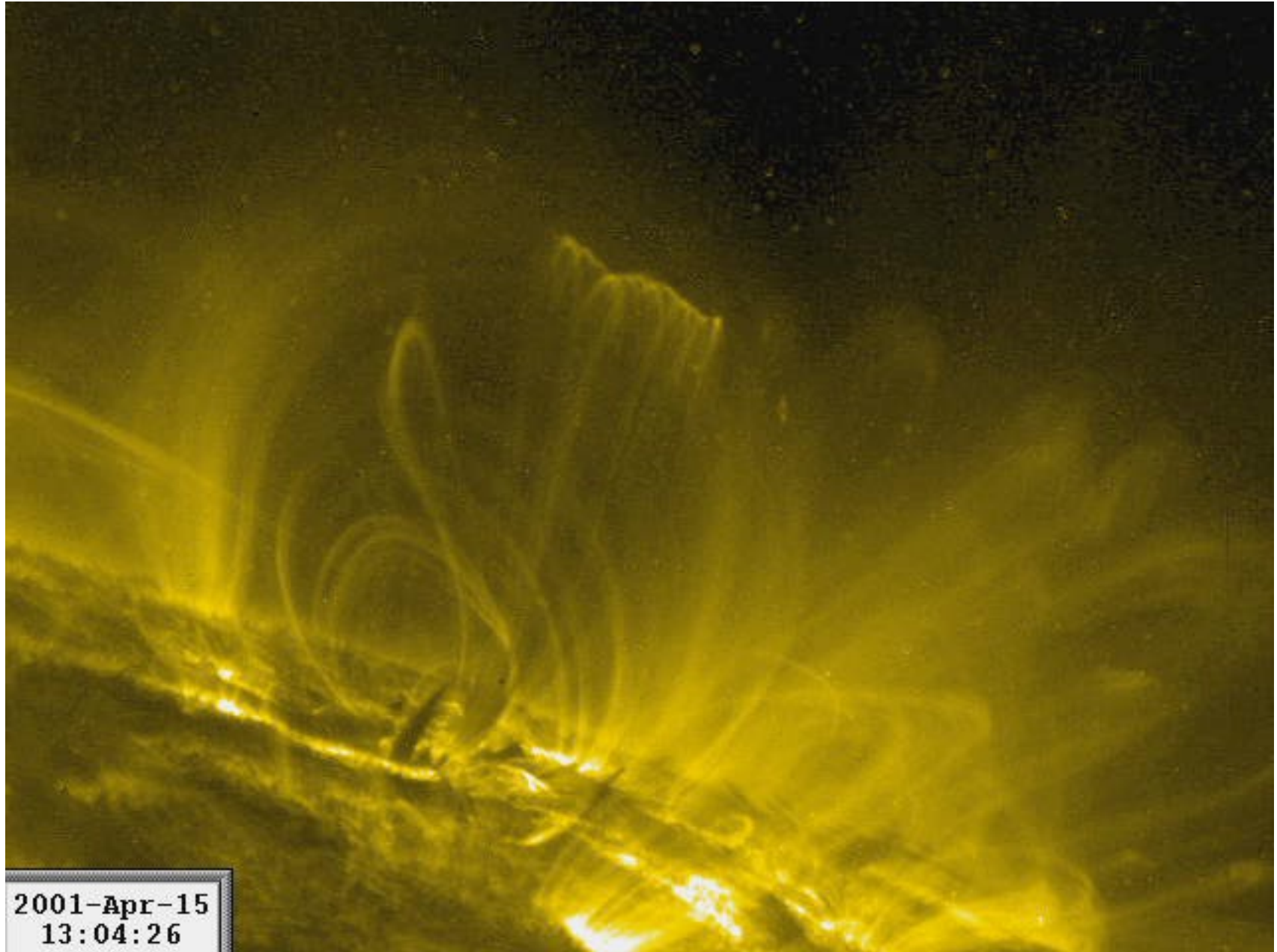
- Sure enough, these clues led Hale to the Zeeman effect.
- But note that there is both a global field, and a local one.

# Routine solar magnetograms



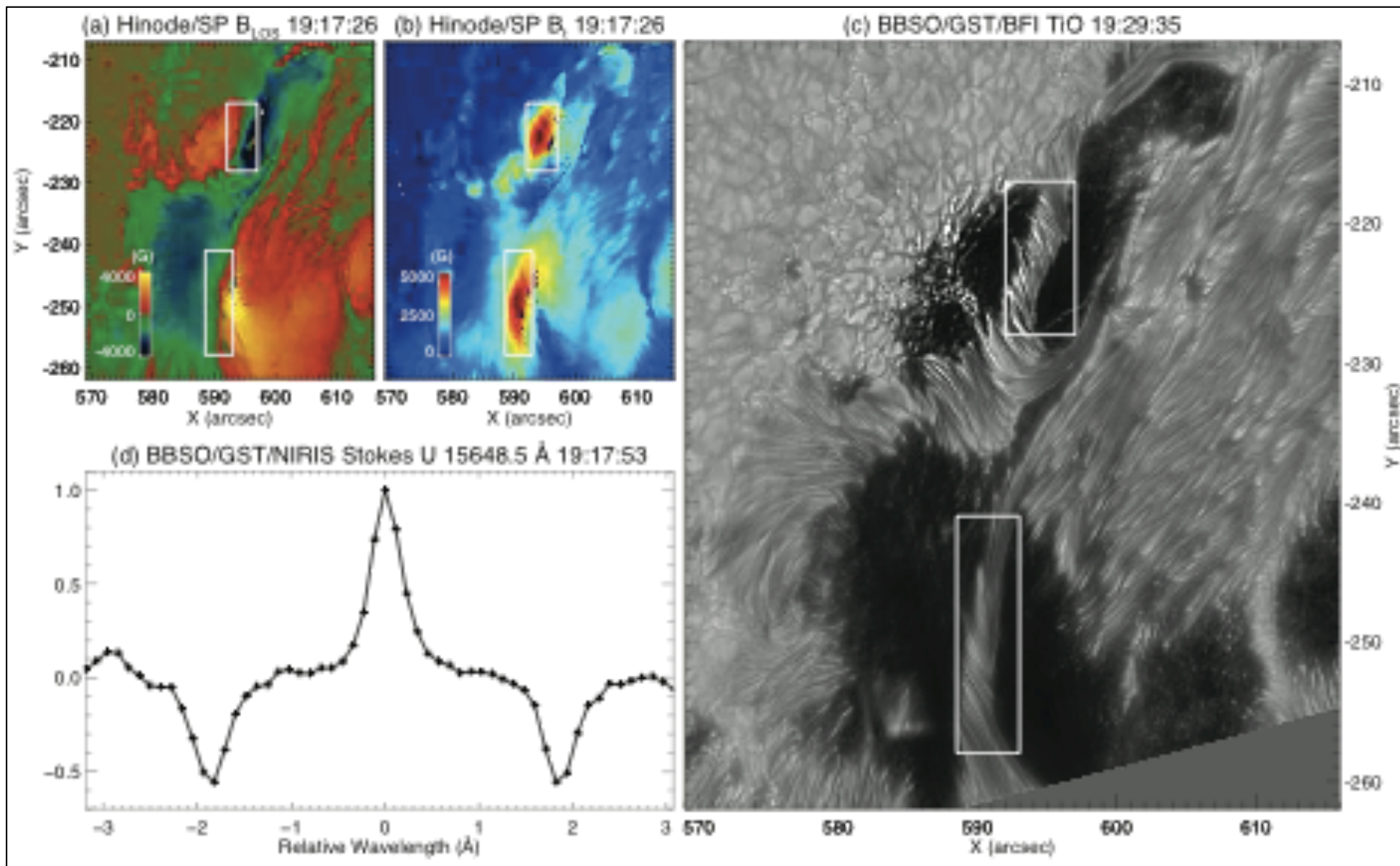


# Magnetic transients II

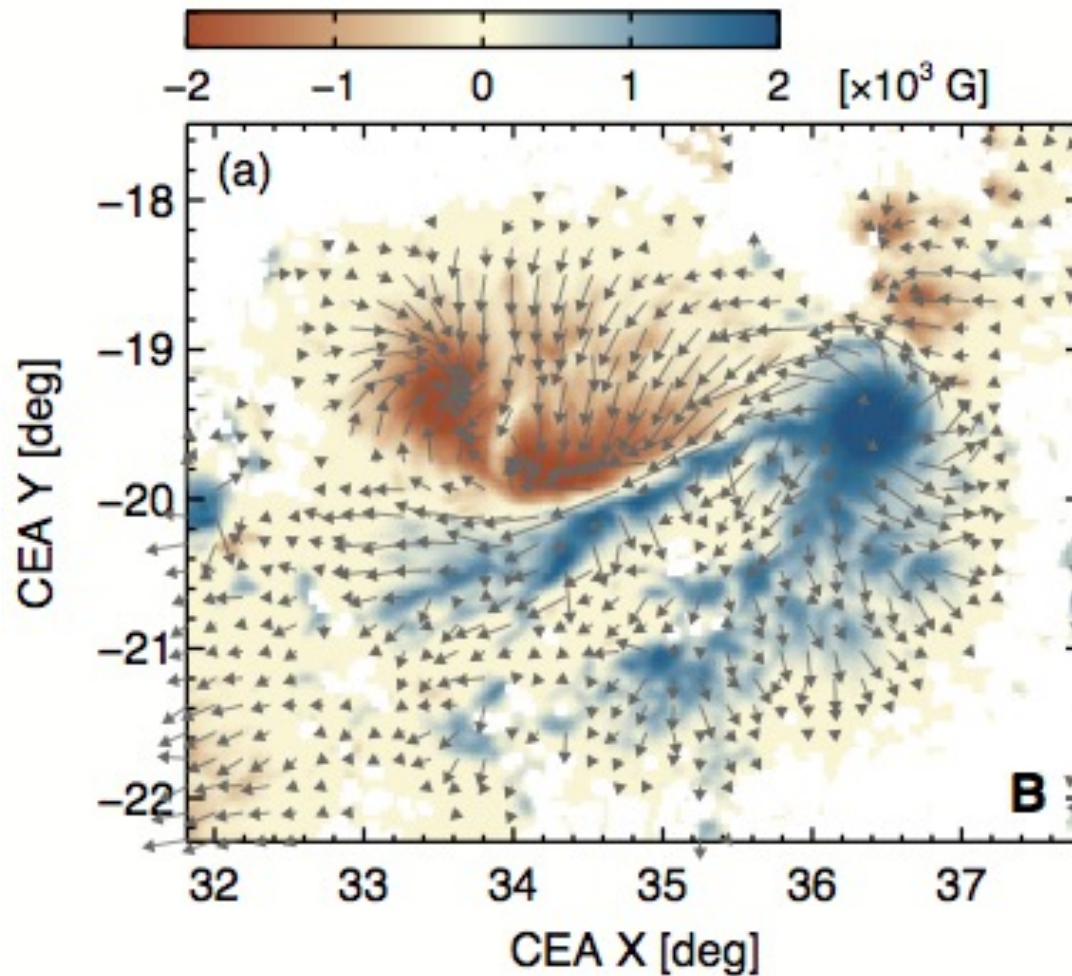


2001-Apr-15  
13:04:26

# Local: an extreme case



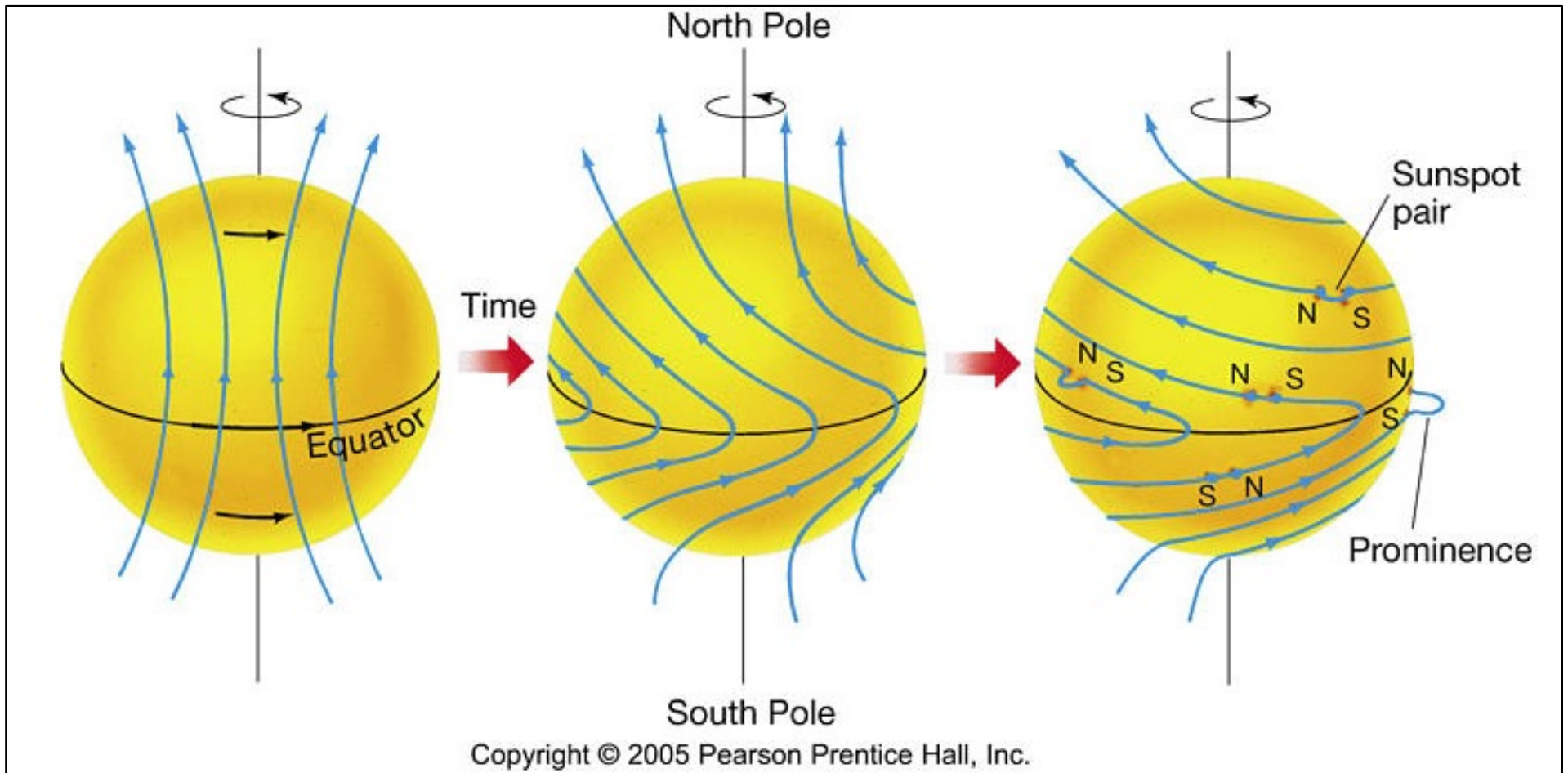
# Vector field representation



With both parallel and perpendicular components, modulo a sign, one can infer the vector **B**.



# Global: the Hale cycle



“Poloidal” fields amplify, due to differential rotation, and become “toroidal”



# The problem of coronal magnetism

- We can use the Zeeman effect in the photosphere to determine the  $\mathbf{B}$  (modulo symmetry-breaking) on a “surface,” but the 3D field is required to understand energetics.
- Unfortunately, the corona is optically thin – polarization signals are weak, and the structure is ill-defined because of the 3<sup>rd</sup> dimension.
- Can we just *extrapolate* from the photospheric boundary into the corona? With full Stokes info, we know the vector  $\mathbf{B}$  in the “plane” of the photosphere.

# Extrapolating the photospheric field

i) Field derived from a scalar potential ( $\nabla \times \mathbf{B} = 0$ )

ii) Linear force-free models, LFF ( $\nabla \times \mathbf{B} = \alpha \mathbf{B}$ )

iii) Non-linear force-free models, NLFF:

$$\nabla \times \mathbf{B} = \alpha(x,y) \mathbf{B}$$

.....

iv) MHD models: zero beta, “cold plasma”;  $P_B \gg P_g$

.....

v) MHD models, multi-fluid MHD

vi) Non-MHD models: any dynamics, actually

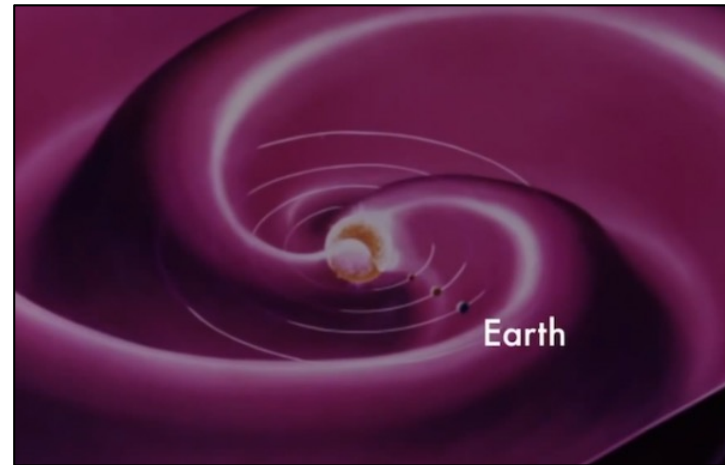
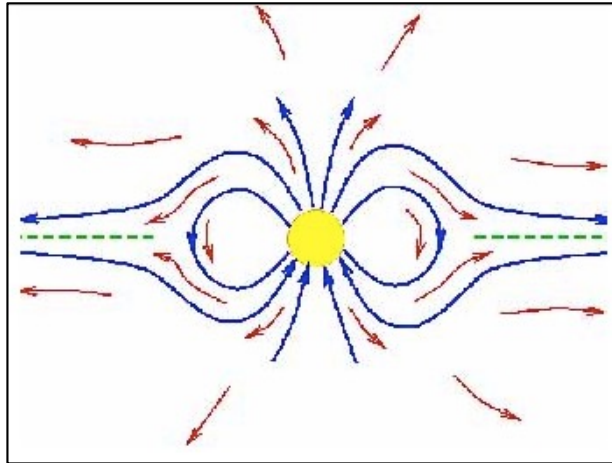
# Potential fields

- Extrapolation would be OK if there were no plasma in the corona, but if that were the case we couldn't see it!
- We could in principle ignore this basic fact and just plow ahead.
- In the absence of currents ( $\nabla \times \mathbf{B} = 0$ )\*, one can uniquely extrapolate the coronal magnetic field via spherical harmonics.
- An example would be to represent the photospheric magnetic field as a set of *magnetic charges* from which a multipole expansion could determine the coronal field.
- In the popular "PFSS" model\*\*, in which the Laplace's equation is solved inside a concentric spherical domain, outside of which the field is assumed to be radial.

\* Thus, solutions of Laplace's equation:  $\nabla^2 \mathbf{B} = 0$

\*\* "Potential Field Source Surface"

# Heliospheric current sheet



- A solar wind, with radial field, violates the potential-field concept of zero current.
- The rotation of the Sun induces a spiral pattern in the heliosphere due to the solar wind.
- Field asymmetry introduces warps (“sectors” at 1 AU) in the structure.

# The Sun last week

www.SolarMonitor.org

Date Search 

3 February 2022

NOAA Search 

← 20220202 ← Week ← Rotation

Today

Rotation → Week → 20220204 →

Main

Far-side

SDO short-wave

SDO long-wave

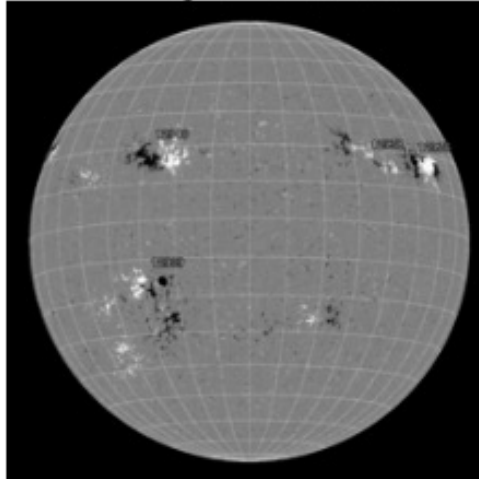
NOAA  
4 Active  
Regions

Flare  
Forecast

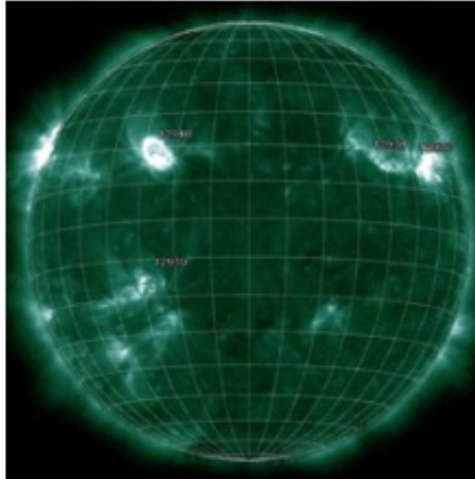
Coronal  
Holes

GOES  
ACE  
SDO/EVE  
Events

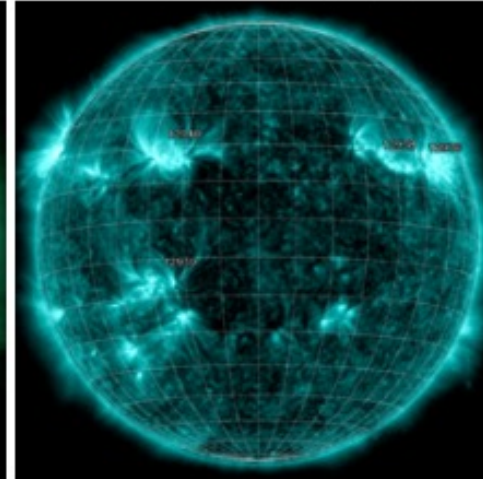
HMI Mag 20220203 16:58



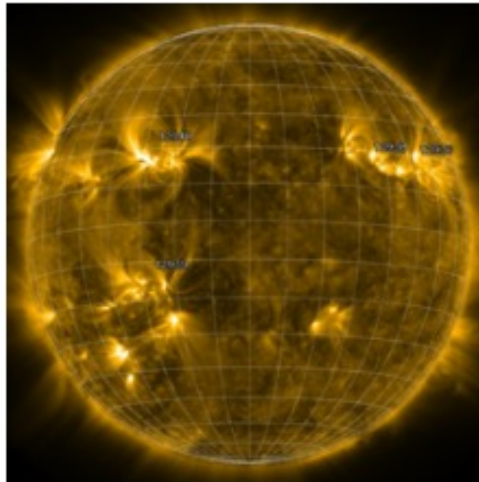
AIA 94Å 20220203 18:13



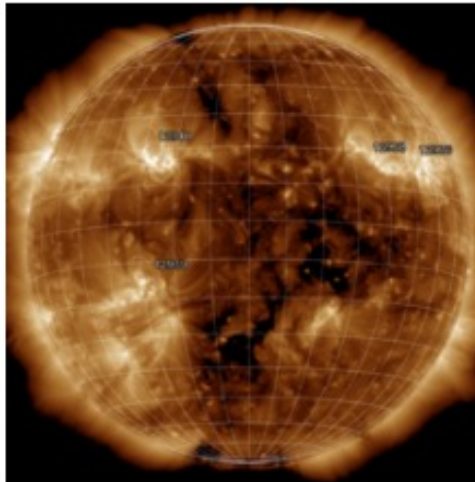
AIA 131Å 20220203 18:15



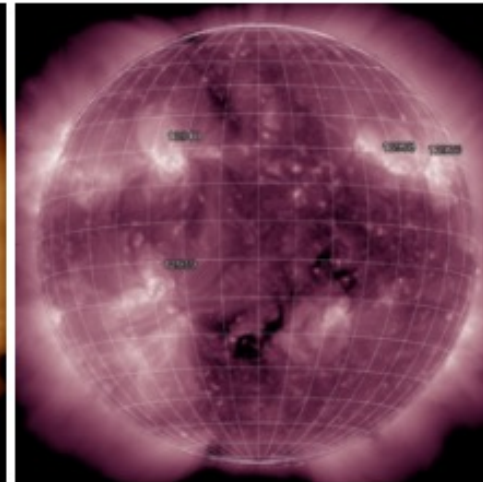
AIA 171Å 20220203 18:13



AIA 193Å 20220203 18:15



AIA 211Å 20220203 18:14





# Two years ago

www.SolarMonitor.org

Date Search 

3 February 2020

NOAA Search 

←20200202 ←Week ←Rotation

Today

Rotation⇒ Week⇒ 20200204⇒

Main

Far-side

SDO short-wave

SDO long-wave

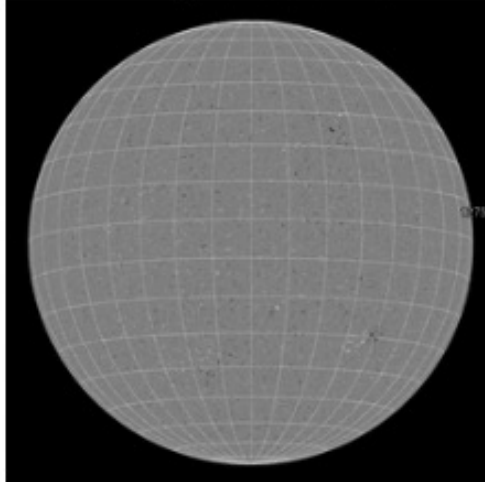
NOAA  
1 Active  
Region

Flare  
Forecast

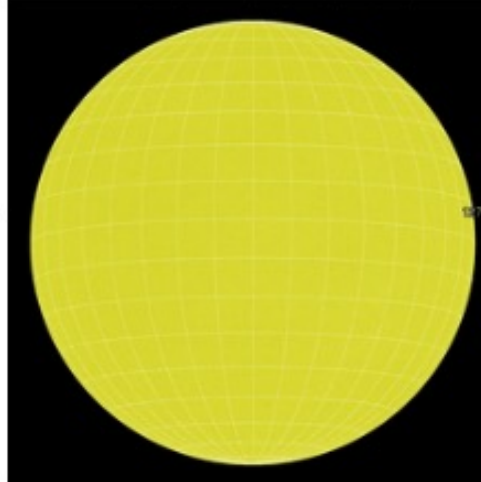
Coronal  
Holes

GOES  
ACE  
SDO/EVE  
Events

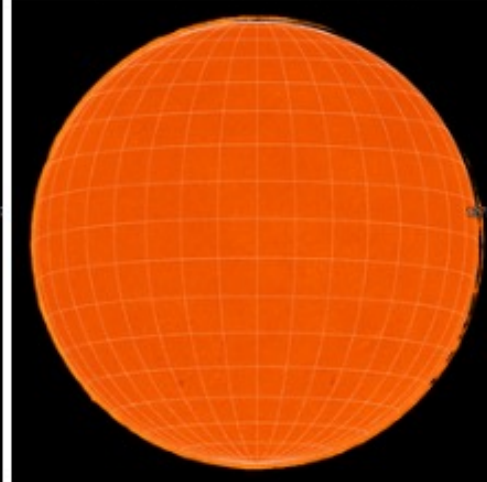
HMI Mag 20200203 19:34



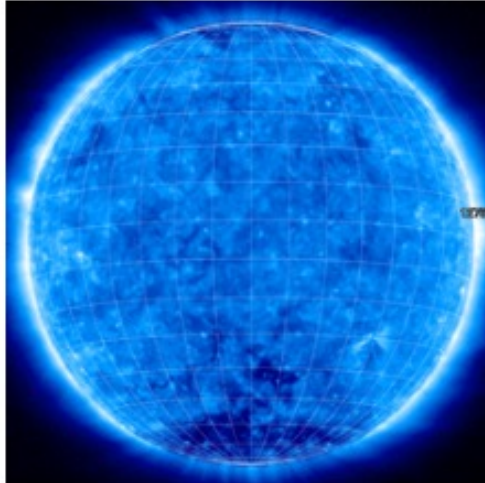
HMI 6173Å 20200203 19:34



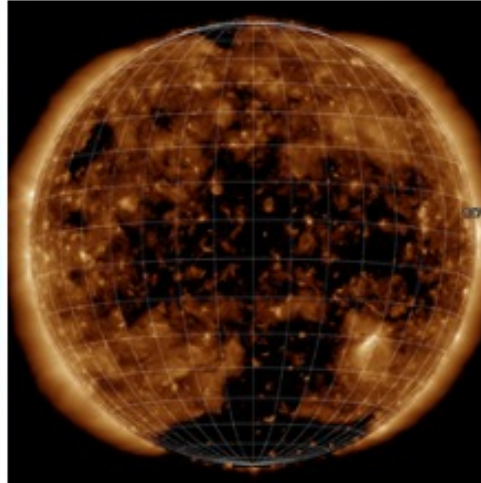
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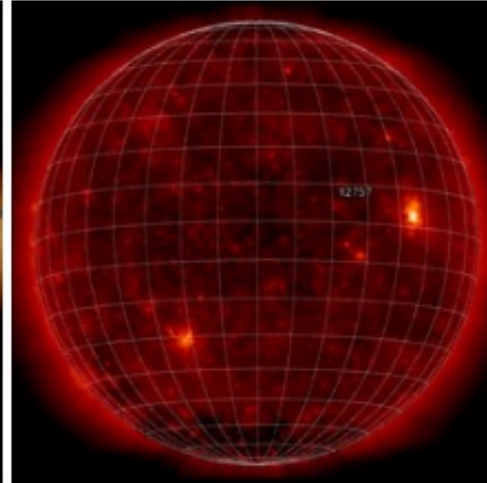
SWAP 174Å 20200203 19:19



AIA 193Å 20200203 20:24



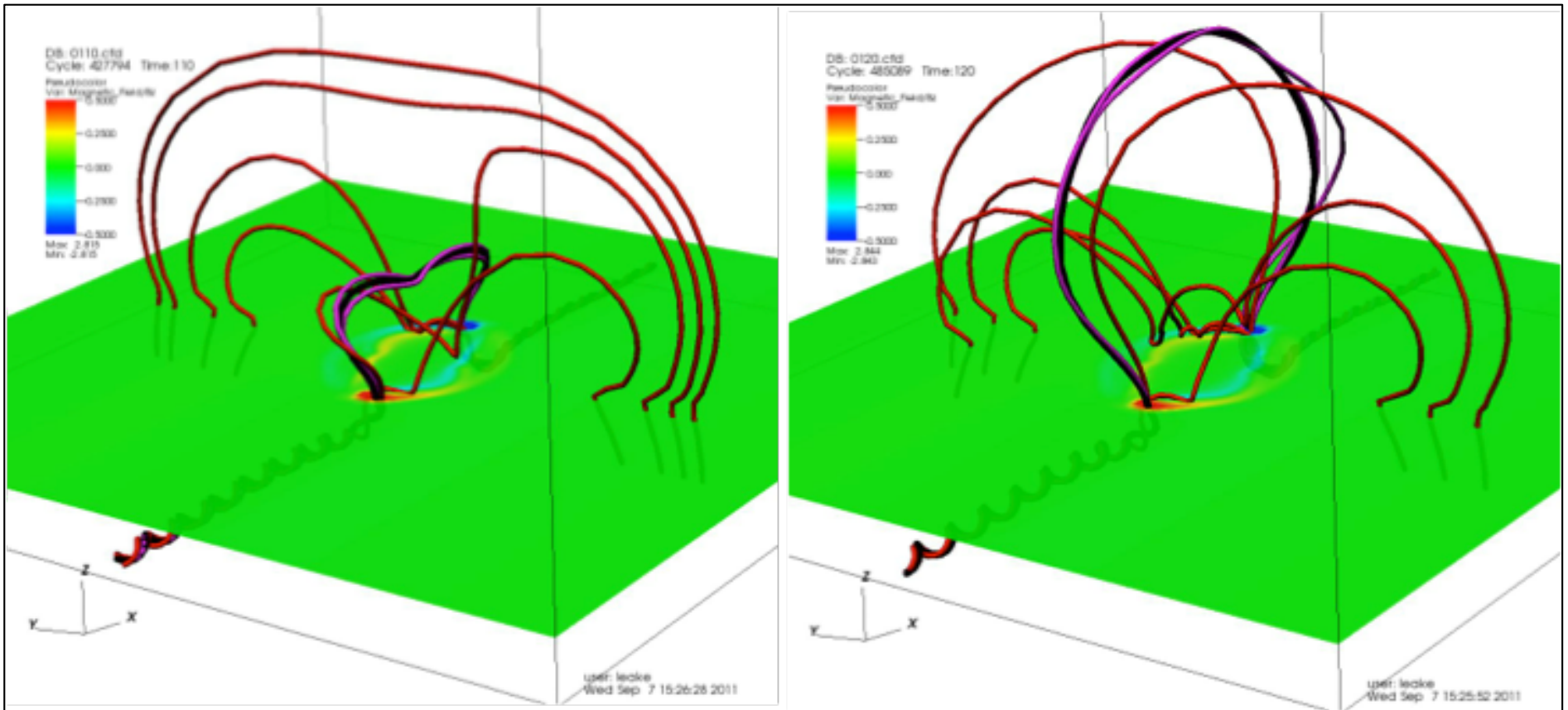
XRT 20200130 05:58



# The stability of the coronal field

- A solar magnetic transient (flare or CME; coronal mass ejection) derives energy from the magnetic field:  $\mathbf{B}^2/8\pi$  (in CGS units). It must become more potential-like as this happens.
- Identifying the plasma instabilities that do this is an open problem now, and of course very important for flare prediction (“space weather”)
  - Ideal MHD instability (no magnetic reconnection), such as the kink instability
  - Resistive instabilities, such as the torus instability or the “tether-cutting” cartoon

# The “torus instability”



- A *flux rope* forms above a *photospheric inversion line*.
- This structure is held in place by overlying field.
- Torok & Kliem (2005) suggest that if this overlying field decreases in strength with height, the structure may blow.



# The “tail wags the dog?”

The corona is orders of magnitude less energetic than the photosphere, and yet...

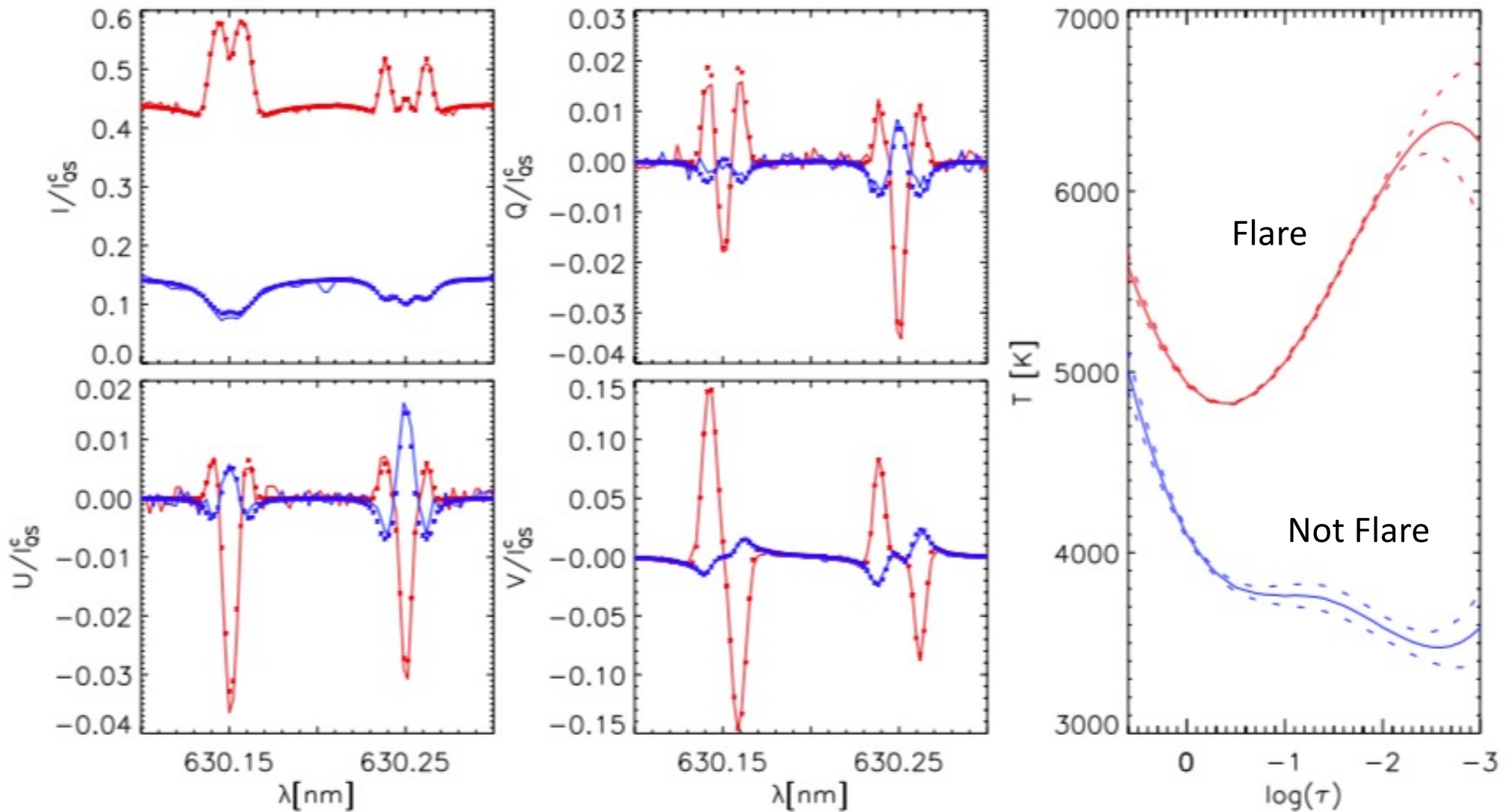
- We see “sunquakes,” acoustic disturbances within the solar interior, following powerful flares.
- Flares may cause sunspots to rotate.

These and other effects have no established theoretical explanation.

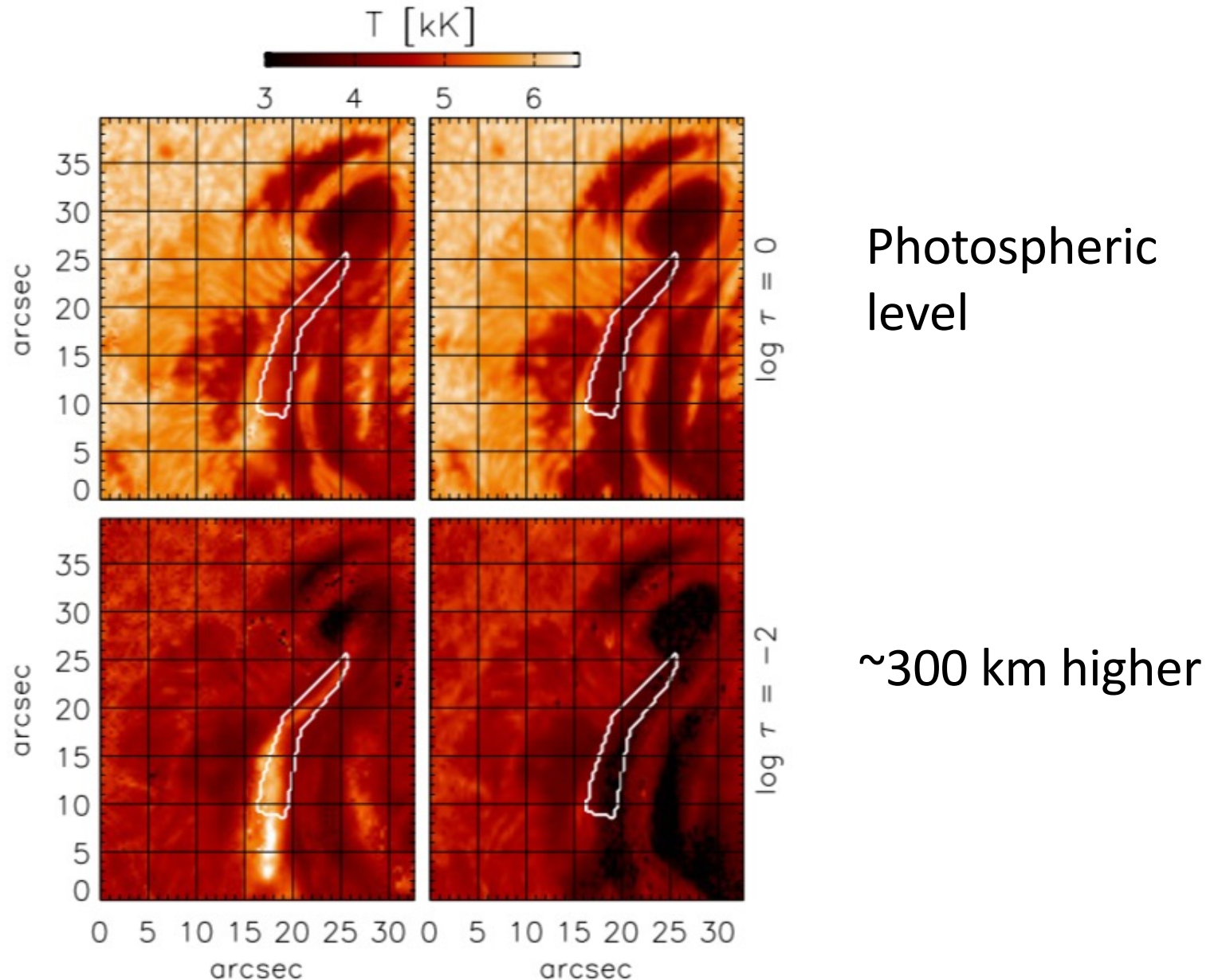
# An exemple research paper

- Jurčák *et al.* 2018, “Heating of the solar photosphere during a white-light flare”
  - The behavior of an actual photospheric spectral line
  - “Line inversions” to obtain quasi-3D structure
  - What the Stokes parameters can tell you
  - How flares might work
- The “SIR” Stoke Inversion code translates line profiles, “forward fitting” T to a coarse 1D map at 5 points over a four-decade range of optical depths: many, many assumptions!

# *Hinode* line profiles and inversion for T

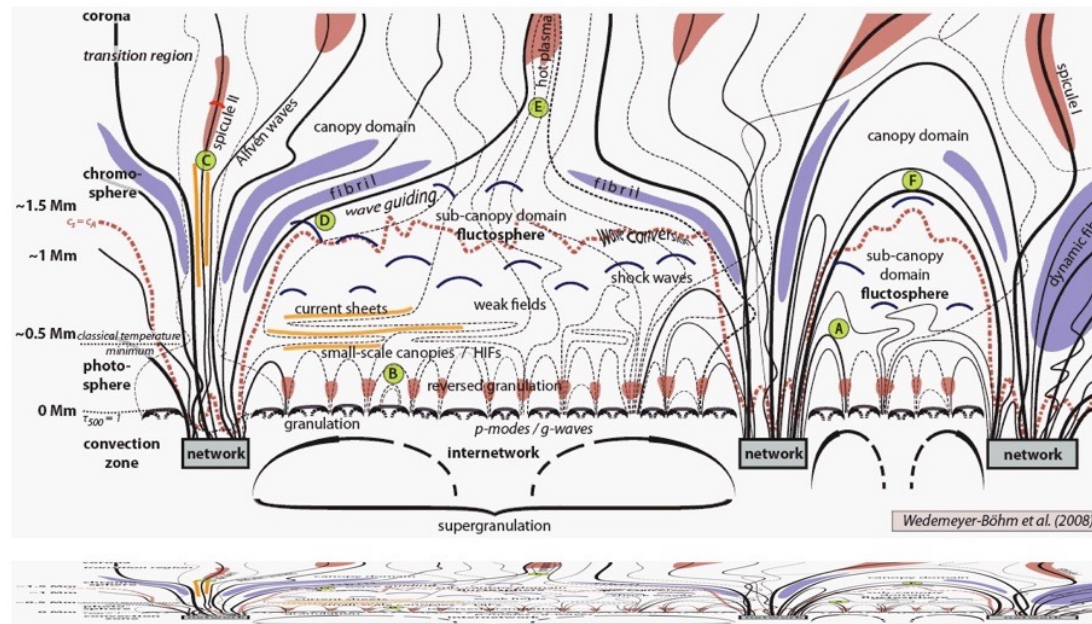


# *Hinode* line profiles and inversion

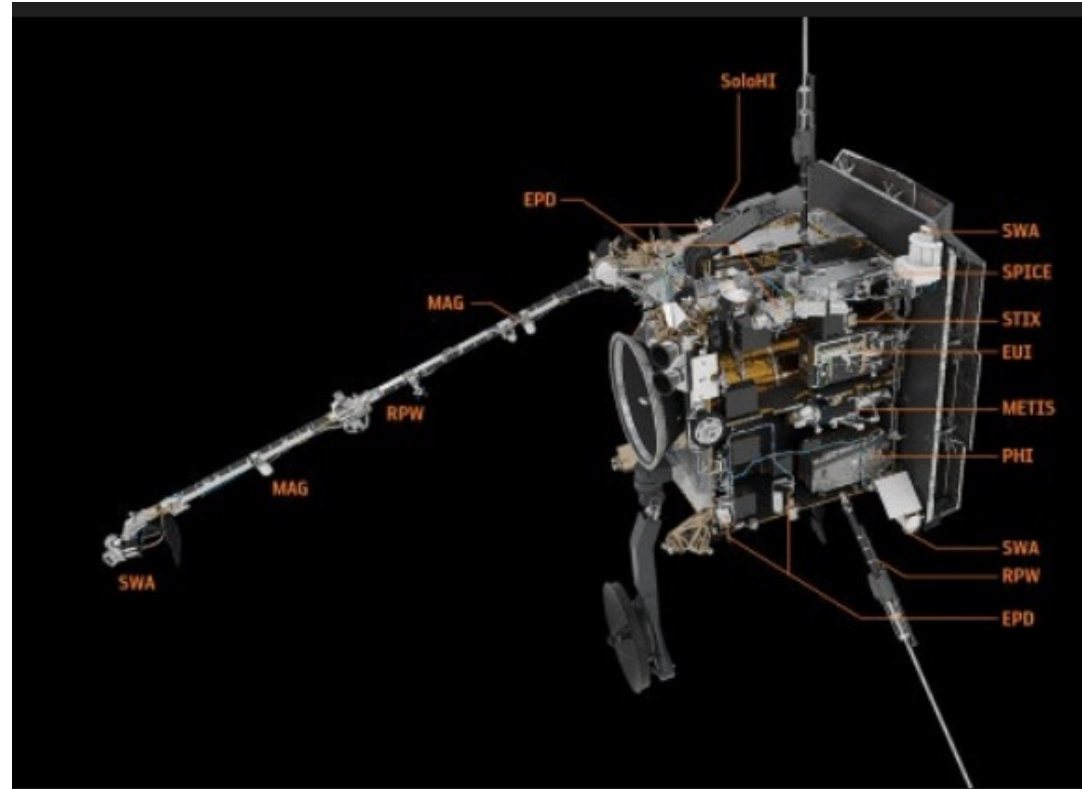
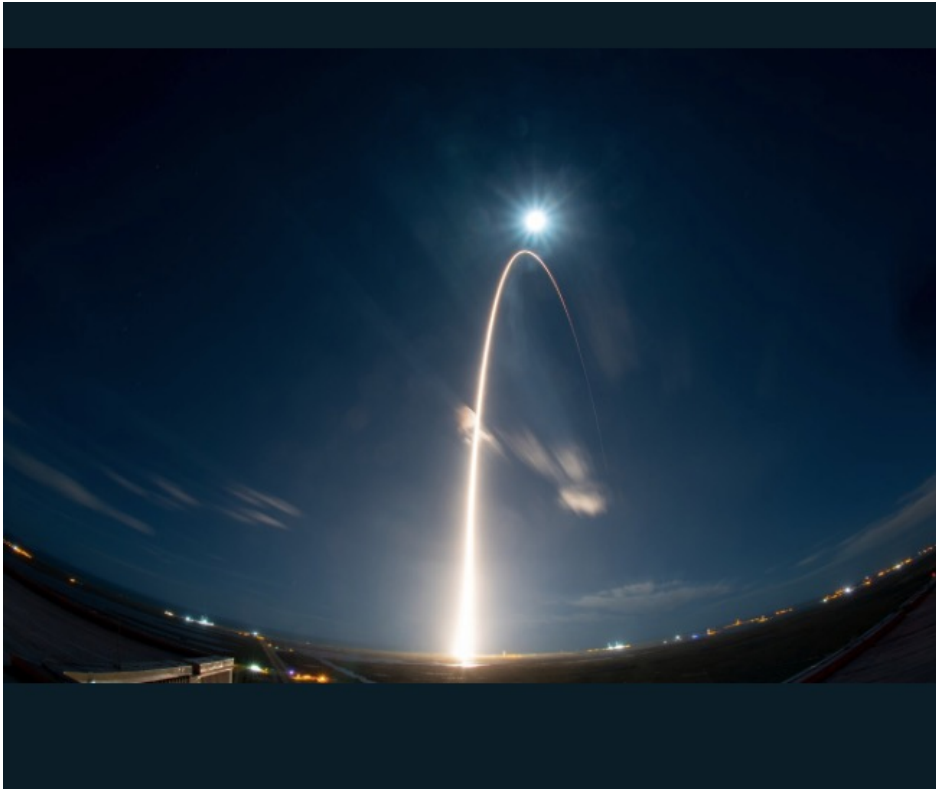


# Conclusions

- Magnetism makes the solar atmosphere interesting from the point of view of plasma physics.
- ALMA (now), DKIST (“first light” already), and Orbiter (just launched) offer wonderful new observational opportunities.



# A new space observatory!



Solar Orbiter launch anniversary Feb. 10!

# Useful homework questions based on this material

- What is the minimum Earth detectable by photometry of a Sun-like star?
- How round is the Sun?
- How big does a solar optical telescope need to be?
- How deep can a Wilson depression be?

*These are questions to be answered by rough approximation, and the necessary facts should be here on the slides. I will post discussion of these items on Files and at*

*<http://www.ssl.berkeley.edu/~hudson/presentations/supa.220207/>*

# If there's time

- Helio- and Asteroseismology



# p-modes, g-modes, and ripples

1941MNRAS...101...367C

## THE NON-RADIAL OSCILLATIONS OF POLYTROPIC STARS

*T. G. Cowling, M.A., D.Phil.*

(Received 1941 November 6)

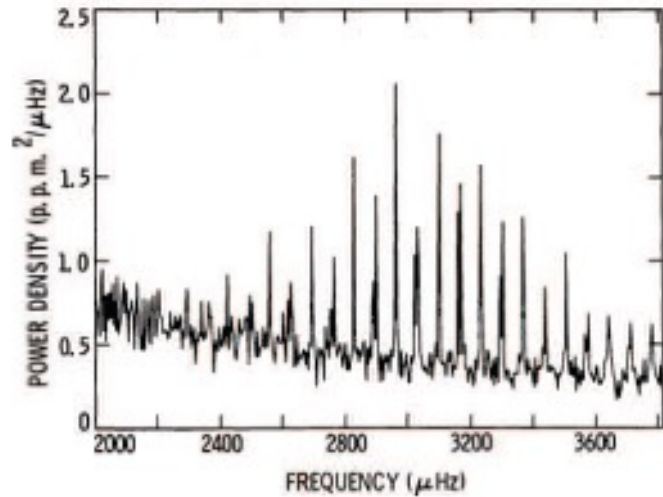
1. The problem of the non-radial oscillations of a fluid globe is of interest in the theory of the tidal distortion of binary stars. If the periods of rotation of the components

### Classification of modes in the Cowling approximation

- p-modes: mainly acoustic standing waves, global
- g-modes: internal gravity waves, evanescent in the convection zone
- f-modes: surface waves

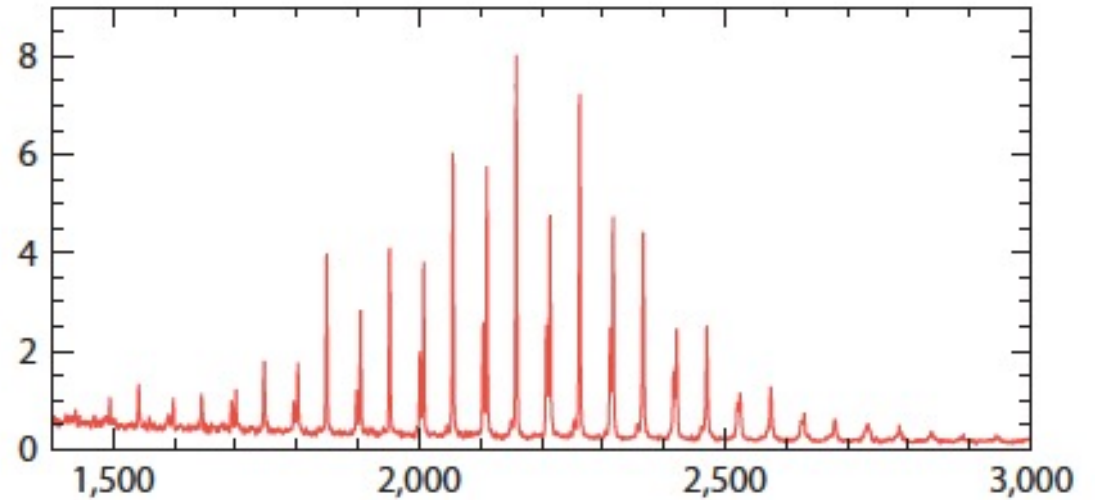
The solar interior also supports acoustic waves excited by flares

# Solar and stellar p-modes



The Sun (Woodard, 1987)

- solar-type
- period  $\sim 27$  d
- $4.85 \times 10^{-6}$  pc
- $m \sim -27$



16 Cyg A (Chaplin & Miglio, 2013)

- solar-type
- period  $\sim 27$  d
- 21 pc
- $m \sim 6$